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Frequency Chirping of Electromagnetic Ion Cyclotron Waves in Earth's Magnetosphere

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Key Points:

- We propose and validate a model of electromagnetic ion cyclotron (EMIC) wave frequency chirping based on the Trap-Release-Amplify model of chorus waves
- The model relates EMIC wave frequency chirping to both wave intensity and background magnetic field inhomogeneity for the first time
- Observations demonstrate a clear decrease in EMIC wave chirping rate with increasing L -shell, consistent with the model prediction

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Abstract Electromagnetic ion cyclotron (EMIC) waves are known to exhibit frequency chirping occasionally, contributing to the rapid acceleration and precipitation of energetic particles in the magnetosphere. However, the chirping mechanism of EMIC waves remains elusive. In this work, a phenomenological model of whistler mode chorus waves named the Trap-Release-Amplify (TaRA) model is applied to EMIC waves. Based on the proposed model, we explain how the chirping of EMIC waves occurs, and give predictions on their frequency chirping rates. For the first time, we relate the frequency chirping rate of EMIC waves to both the wave amplitude and the background magnetic field inhomogeneity. Direct observational evidence is provided to validate the model using previously published events of chirping EMIC waves. Our results not only provide a new model for EMIC wave frequency chirping, but more importantly, they indicate the potential wide applicability of the underlying principles of TaRA model.

Plain Language Summary Rapid change of wave frequency, or frequency chirping, can frequently be observed in space and laboratory plasmas. Chirping waves generally appear as discrete and narrowband elements and can cause rapid acceleration or scattering of energetic particles through nonlinear interactions. Correspondingly, the physical mechanism of frequency chirping has attracted considerable research interest. This work aims to explain how electromagnetic ion cyclotron (EMIC) wave frequency chirping arises, which remains an open question. We apply a previously developed model of whistler mode chorus waves named the Trap-Release-Amplify (TaRA) model to chirping EMIC waves, and make a series of chirping rate predictions. In particular, we find that after taking into account all the different stages of wave excitation, chirping rate of EMIC waves should be related to both wave amplitude and background magnetic field inhomogeneity. A comparison between the theoretical chirping rates and observations using previously published EMIC wave chirping events shows good consistency. The results provide both a new explanation for EMIC wave frequency chirping and an indirect test of the underlying principles of the TaRA model.

1. Introduction

Electromagnetic ion cyclotron (EMIC) waves have been demonstrated to play important roles in dynamics of radiation belt electrons and ring current protons. For example, scattering induced by EMIC waves is considered as one of the most important drivers of relativistic electron precipitation into the atmosphere (Blum et al., 2015; Denton et al., 2019; Drozdov et al., 2022; Hendry et al., 2017; Kersten et al., 2014; Usanova et al., 2014), via resonant (Bingley et al., 2019; Meredith et al., 2003; Ni et al., 2015; B. Wang et al., 2016), and nonresonant (X. An et al., 2022; Chen et al., 2016) wave-particle interactions. EMIC waves are also responsible for rapid decay of ring current protons during geomagnetic storms (Jordanova et al., 2001, 2007; Sakaguchi et al., 2008). Moreover, EMIC waves can transfer energy effectively between different particle populations through heating cold electrons and ions (Kitamura et al., 2018; Ma et al., 2019; Zhou et al., 2013). Correspondingly, understanding EMIC wave generation and the relevant wave-particle interaction processes could be helpful to studies about a wide range of magnetospheric phenomena.

Although the linear instability of EMIC waves is well understood and typically related to temperature anisotropy in the inner magnetosphere (Gary et al., 1996; Gendrin et al., 1984), some EMIC waves exhibit nonlinear frequency chirping, in the form of spontaneous rising-tone emissions (Mursula et al., 1994; Pickett et al., 2010).

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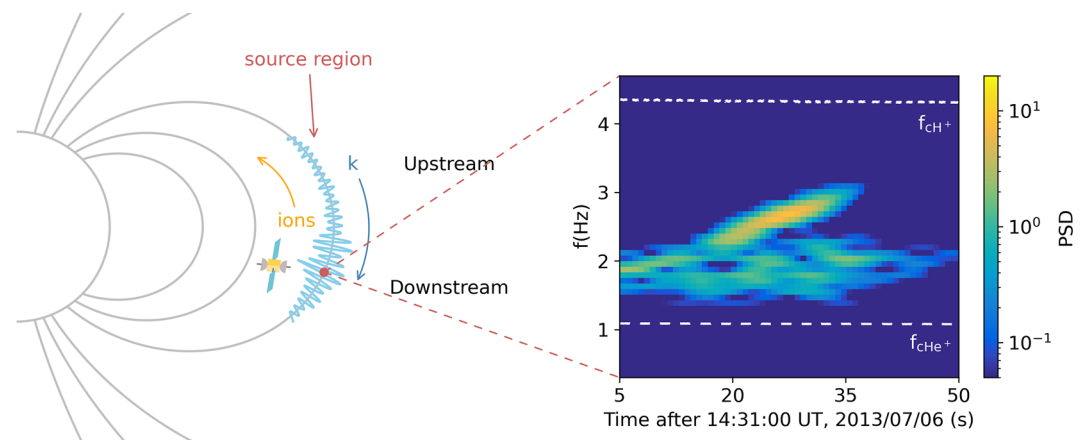


Figure 1. An illustration of our electromagnetic ion cyclotron wave frequency chirping model. As indicated by the satellite icon, chirping elements are usually observed downstream of the equator, where they have been fully amplified through nonlinear wave-particle interactions. The rising-tone element shown in the right panel was observed by RBS-P-A satellite at 14:31 UT, 06 July 2013.

Such frequency chirping has also been observed in several other wave modes, including whistler mode chorus waves (Tsurutani & Smith, 1974), magnetosonic waves (Boardsen et al., 2014; Fu et al., 2014), electron cyclotron harmonic waves (S. Liu et al., 2023; Shen et al., 2021; Teng et al., 2021) in the magnetosphere and Alfvén waves (Heidbrink, 2008; Heidbrink & Sadler, 1994; McGuire et al., 1983) in fusion plasmas. These chirping waves generally consist of discrete packets that are narrowband and quasi-coherent (Tsurutani et al., 2009). Interaction with these chirping modes often results in rapid transport of energetic particles in phase space (Albert & Bortnik, 2009; Artemyev et al., 2016; Chen & Zonca, 2007; Grach & Demekhov, 2020; Grach et al., 2022; McGuire et al., 1983; Tao, Bortnik, et al., 2012; White et al., 1983; Zhang et al., 2018; Zonca et al., 2005), affecting space weather or deteriorating particle confinement in fusion devices. Therefore, there is significant research interest in understanding the physical mechanism of frequency chirping in both communities of space and laboratory plasmas.

While there are several observational studies about EMIC wave chirping (Grison et al., 2013; Mursula, 2007; Mursula et al., 1994; Nakamura et al., 2016; Pickett et al., 2010; Y. Wang et al., 2023), theoretical studies are quite limited. Hybrid simulations have clearly demonstrated that EMIC wave frequency chirping is caused by nonlinear processes (Shoji & Omura, 2013). The sequential triggering model by Omura and Nunn (2011) and Shoji et al. (2017), originally developed for chorus waves, has been applied to explain EMIC wave frequency chirping in simulations and observations (Omura et al., 2010). These studies confirmed that the frequency chirping rate is proportional to wave amplitude, a feature from the nonlinear generation process.

In this work, we propose a new model of EMIC wave frequency chirping based on the recently proposed “Trap-Release-Amplify” (TaRA) model of whistler mode chorus waves (Tao et al., 2021), considering similar nonlinear wave-particle interaction processes in the chirping of chorus and EMIC waves (Section 2). Different from previous models (Omura et al., 2010; Trakhtengerts & Demekhov, 2007), our model relates the chirping rate of EMIC waves not only to the wave amplitude but also to the background magnetic field inhomogeneity. Two chirping rate predictions are given in Section 2 and compared with observations in Section 3. The comparison shows good agreement, suggesting the validity of our model and that the same underlying principle exists between chorus wave and EMIC wave frequency chirping. Our results, therefore, not only provide a different way of understanding EMIC wave frequency chirping but also give new insights into the chirping mechanisms of other wave modes in both space and laboratory plasmas.

2. A Model of EMIC Wave Frequency Chirping

We illustrate our chirping model of EMIC waves in Figure 1. Each element of the chirping EMIC wave is represented by a narrowband quasi-coherent wave packet, with a frequency that increases nearly continuously from ω_{\min} to ω_{\max} . We further adopt the basic principle of the TaRA model of chorus and divide the generation region of

EMIC waves into upstream and downstream regions separated by the equator. As the generated part of the EMIC wave packet propagates downstream of the equator, it constantly encounters fresh resonant ions moving in the opposite direction. If the wave is quasi-coherent and intense enough, some of the ions will get phase-trapped by the wave packet. Because of Liouville's theorem, the phase space density along a particle's trajectory is conserved. The resonant interaction between ions and EMIC waves results in phase-trapped ions moving from low phase space density region to high phase space density region, forming a localized phase space hole (Nunn, 1974; Tao et al., 2020), which has been demonstrated by computer simulations in Shoji and Omura (2011) and Shoji and Omura (2013). As the ions travel across the wave packet, they will eventually get released in the upstream region where the wave amplitude is small. However, these released ions still retain certain phase correlation, resulting in a current and selective amplification of new emissions from the nearly continuous spectrum of background EMIC waves. The condition for the selective amplification is mathematically expressed using the phase-locking condition $d^2\zeta/dt^2 = 0$. Here, ζ is the wave-particle interaction phase angle between the wave magnetic field $\delta\mathbf{B}$ and the ion perpendicular velocity \mathbf{v}_\perp with respect to the background magnetic field. Such a selection rule guarantees maximum power transfer from ions to waves by holding the resonance condition $d\zeta/dt = 0$ for the longest time possible. Note that fresh ions are continuously entrapped in the downstream and detrapped in the upstream, allowing frequency chirping from ω_{\min} to ω_{\max} .

Based on the above chirping model, two different chirping rates can then be derived. From the nonlinear wave-particle interaction theories of parallel propagating EMIC waves, the second-order time derivative of the wave-particle interaction phase angle ζ could be written as (Omura et al., 2010)

$$\frac{d^2\zeta}{dt^2} = \omega_{tr}^2 \sin \zeta + (R_1 + R_2), \quad (1)$$

where

$$R_1 = \left(1 - \frac{v_r}{v_g}\right)^2 \frac{\partial\omega}{\partial t}, \quad (2)$$

$$R_2 = \left[\left(\frac{v_\perp^2}{2v_p} + \frac{v_r^2}{v_g} \right) \frac{\omega}{\Omega_i} - v_r \right] \frac{\partial\Omega_i}{\partial s}, \quad (3)$$

assuming constant cold plasma density along the field line. Here R_1 and R_2 represent the effects of frequency chirping and background magnetic field nonuniformity, respectively, and s is the distance along a field line from the equator. The parameter R , widely used by other studies (Nunn, 1974; Vomvoridis & Denavit, 1979), equals $(R_1 + R_2)/\omega_{tr}^2$. In Equation 1 above, $\omega_{tr} = \sqrt{k v_\perp \Omega_w}$ is the phase-trapping frequency, with k the wavenumber and $\Omega_w \equiv q_i \delta B / m_i c$. Here q_i is the ion charge, m_i is the ion mass and c is the speed of light in vacuum. In Equations 2 and 3, $v_r = (\omega - \Omega_i)/k$ is the cyclotron resonance velocity, $v_g = \partial\omega/\partial k$ is the wave group velocity, $v_p = \omega/k$ is wave phase velocity, and $\Omega_i \equiv q_i B / m_i c$ is the non-relativistic ion cyclotron frequency.

The first chirping rate is deduced from nonlinear wave-particle interaction theories and is same as the one obtained by the previous model of EMIC wave chirping. At the equator, $R_2 \propto \partial\Omega_i/\partial s \sim 0$. We then arrive at the relation between chirping rates and wave amplitudes as in earlier studies (Omura et al., 2008, 2010; Vomvoridis et al., 1982; Zonca et al., 2022):

$$\frac{\partial\omega}{\partial t} = R \left(1 - \frac{v_r}{v_g}\right)^{-2} \omega_{tr}^2 \Big|_{s=0} \propto \delta B. \quad (4)$$

Effective power transfer is found to occur for R to be about 0.5 (Omura et al., 2008; Vomvoridis et al., 1982; Zonca et al., 2021). This chirping rate has been obtained before, and for convenience, it will be called the nonlinear chirping rate.

Applying the principle of the TaRA model of chorus to EMIC waves allows us to obtain a new expression of the chirping rate. At the upstream source location s_0 , phase-trapped ions are released to amplify new waves from the pre-existing thermal noise spectrum, which means that δB is small or ω_{tr}^2 is negligible compared with R_2 in Equation 1. The phase-locking condition is then reduced to

$$\frac{d^2\zeta}{dt^2} \approx R_1 + R_2 = 0, \quad (5)$$

leading to

$$\frac{\partial\omega}{\partial t} = - \left(1 - \frac{v_r}{v_g}\right)^{-2} \left[\left(\frac{v_{\perp}^2}{2v_p} + \frac{v_r^2}{v_g} \right) \frac{\omega}{\Omega_i} - v_r \right] \frac{\partial\Omega_i}{\partial s} \Big|_{s=s_0}. \quad (6)$$

This equation demonstrates the dependence of chirping rate on background magnetic field inhomogeneity and is expected to be evaluated at the wave source location upstream of the equator. An order-of-magnitude estimate of the source location s_0 is that $s_0 = (2\pi|v_r|/\xi\Omega_{i0})^{1/3}$ (Helliwell, 1967), corresponding to a shift of π radian of the wave particle interaction phase angle ζ from the equator assuming linear motion of ions. Here we approximate the background magnetic field B near the equator as $B = B_0(1 + \xi s^2)$, and ξ is a measure of the magnetic field inhomogeneity.

So far, two chirping rate expressions have been derived: Equation 4 at the equator and Equation 6 in the source location s_0 . The new model of EMIC wave chirping, therefore, predicts that the chirping rate of EMIC waves is not only related to wave amplitude at the equator, but also to the background magnetic inhomogeneity. We must emphasize that, although the two equations look different and have different origins of physical mechanisms, they are consistent and both are correct at different stages of wave excitation.

3. Comparing the Model to Observations

We now provide a direct comparison with observations to test the above two EMIC wave chirping rate predictions using all the previously published events we are aware of. Different from whistler mode chorus waves, there are not many observed events of chirping EMIC waves. The only selection rule we apply is that the magnetic latitude of the event should be less than 5° for Equation 4 and less than 10° for Equation 6 to avoid being too far away from the equator. We select events closer to the equator for Equation 4 because wave amplitude could vary significantly as wave propagates from the equator to high latitudes. In total, we have 15 EMIC wave rising-tones for Equation 6 and 11 for Equation 4, all of which are in-situ observations of spontaneously excited EMIC waves with clear frequency chirping elements. These observations were made by different spacecraft including Cluster (Escoubet et al., 1997), Van Allen Probes (Mauk et al., 2013), and Time History of Events and Macroscale Interactions during Substorms (THEMIS, Angelopoulos (2008)), during different time periods and at a wide range of radial distances. Therefore, these selected events should be a good representation of EMIC wave chirping elements in the magnetosphere. Their brief information is summarized in Table 1.

Before calculating the theoretical chirping rates, we describe the method we use to estimate wavenumber k . Although it is typical to obtain k from the cold plasma dispersion relation, this approach could become very inaccurate at frequencies near ion gyrofrequencies. Furthermore, the heavy ion (He^+ and O^+) densities are sometimes difficult to determine or even missing in satellite data. Using empirical heavy ion compositions is inappropriate here, as different events might correspond to very different cold plasma parameters. To avoid this problem, we adopt the wavenumber analysis method proposed by Chen et al. (2019), which allows us to extract $k(\omega)$ directly from the observed waveforms. The method involves three steps for a chirping element like the one shown in Figure 2a. First, we determine the evolution of wave frequency with time from the wave spectrogram. In this step, we only select points with large enough power spectral densities and small enough wave normal angles. Specifically, we require that magnetic power spectral density $\text{PSD} > 0.01\text{PSD}_{\max}$, in which PSD_{\max} is the maximum PSD in the chirping element, and wave normal angle $\Psi < 45^\circ$. The selected points are shown in Figure 2b. Second, we use the singular value decomposition method (Santolík et al., 2003) to solve for k at the selected points, using five components of the electromagnetic fields ($B_x, B_y, B_z, E_x,$ and E_z , in the GSE coordinate system). The results are plotted against ω in Figure 2c. Finally, we fit all the points with a quadratic function: $k = a\omega^2 + b\omega + c$ to obtain a single wavenumber at a certain frequency. For a particular element, we use $\omega_{\text{mid}} = (\omega_{\min} + \omega_{\max})/2$ and the corresponding $k(\omega_{\text{mid}})$ to estimate its theoretical chirping rate. This method of estimating k does not rely on the information of plasma components; however, one potential concern is that antennas onboard spacecraft actually measure E/Z , where Z is the complex transfer function of the interface between the electric antennas and the plasma. Santolík and Parrot (2000) and Parrot et al. (2001) demonstrated that Z is highly variable and

Table 1

Brief Information of the 15 Observational Events, Arranged in the Order of Time of Occurrence, Which Is a 10-Minute-Long Vicinity of the Interested Chirping Element

	Time of occurrence (UT)	L -shell	MLT (hr)	MLAT (deg)	Frequency range (Hz)	Observed by	First reported by
1	07:55–08:05, 2002/03/30	4.45	22.3	−3.4	1.56–2.87	Cluster 4	Pickett et al. (2010)
2	00:10–00:20, 2003/03/27	4.17	22.6	−1.78	1.6–3.46	Cluster 4	Grison et al. (2013)
3	09:05–09:15, 2008/04/16	7.2	17.8	−8.82	0.31–0.59	THEMIS A	Nakamura et al. (2015)
4	17:40–17:50, 2008/10/11	6.98	12	0.2	0.5–0.97	THEMIS A	Nakamura et al. (2015)
5	18:30–18:40, 2010/06/25	8.03	17.6	0.08	0.28–0.5	THEMIS A	Nakamura et al. (2015)
6	17:35–17:45, 2010/07/11	7.83	16.5	3.7	0.38–0.63	THEMIS E	Nakamura et al. (2014)
7	14:20–14:30, 2010/09/09	8.33	13.2	4.83	0.5–0.97	THEMIS D	Nakamura et al. (2014)
8	13:20–13:30, 2010/09/24	8.27	12.4	4.8	0.47–0.84	THEMIS D	Nakamura et al. (2015)
9	08:35–08:45, 2011/09/25	8.87	17.9	−2.9	0.25–0.41	THEMIS A	Nakamura et al. (2015)
10	14:25–14:35, 2013/07/06	4.05	18.1	2.45	2.25–3.13	RBSP-A	Chen et al. (2019)
11	19:50–20:00, 2013/11/29	5.78	15	2.82	0.31–0.45	RBSP-B	Y. Wang et al. (2023)
12	11:30–11:40, 2014/02/23	6.68	14.9	−1.54	0.75–1.19	THEMIS D	N. Liu et al. (2020)
13	23:35–23:45, 2014/05/04	5.83	9.99	−5.03	0.94–1.5	RBSP-A	Y. Wang et al. (2023)
14	10:15–10:25, 2015/12/22	5.4	13.3	−8.02	1.06–1.94	RBSP-A	Sigsbee et al. (2020)
15	12:15–12:25, 2017/09/07	5.68	13.7	5.63	0.88–1.75	RBSP-A	Zhu et al. (2020)

Note. Event 11 is a helium-band wave, while the others are hydrogen-band waves.

event-dependent for waves above 1 kHz. On the other hand, for EMIC waves with frequencies around 1 Hz, Grison et al. (2014) concluded that $Z \approx 1$ is appropriate for Cluster data. As this $Z \approx 1$ value is also consistent with the Van Allen Probes results of Chen et al. (2019), it is also the assumption adopted by our study.

Figure 3 shows comparisons between observational (Γ_{ob}) and theoretical chirping rates. Figure 3a shows the comparison for $\Gamma(\delta B)$, Equation 4, and Figure 3b for $\Gamma(\partial B/\partial s)$, Equation 6. When estimating the theoretical chirping rates, we calculate δB by integrating over the wave power spectral density. Both the equatorial value B_0 and the inhomogeneity factor ξ of the background magnetic field are derived by fitting data given by the T89 magnetic field model (Tsyganenko, 1989) with a parabolic function $B = B_0(1 + \xi s^2)$. The perpendicular velocity v_{\perp} is estimated from the resonant velocity v_r and a pitch angle $\alpha = 70^\circ$, following that nonlinear phase-trapping occurs most easily for pitch angles between 65° and 75° (Inan et al., 1978). For observational chirping rates, we simply use $\Gamma_{\text{ob}} = (\omega_{\text{max}} - \omega_{\text{min}})/\Delta t$ with Δt the duration of element. Each point represents an event in Table 1, with the corresponding satellite missions and L -shell values categorized by different markers and colors, respectively. The shaded region represents a maximum difference of a factor of two. Figure 3 shows that, for most events (8 out of 11 for Figure 3a and 13 out of 15 for Figure 3b), the differences between observation and both theoretical

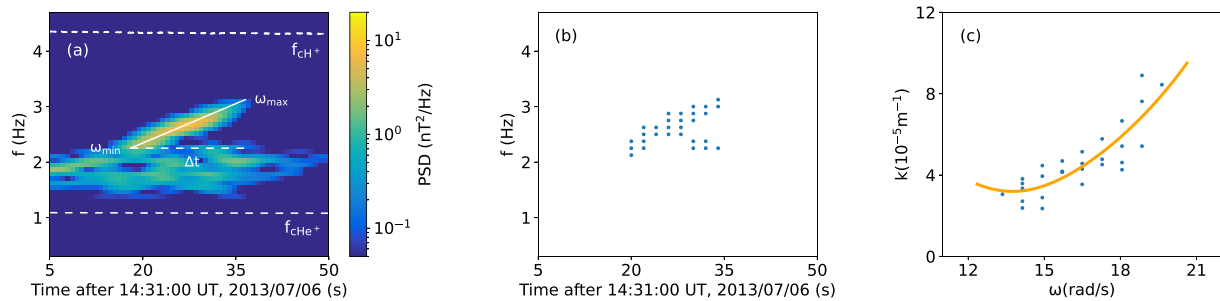


Figure 2. A demonstration of the wavenumber estimation method. (a) The spectrogram of the chirping element, Event 10 of Table 1. (b) Points in the spectrogram which satisfy all selection rules described in the text. (c) Wavenumber k solved with the singular value decomposition method (the blue dots) and a quadratic fit (the orange curve) of them as a function of frequency ω . The minimum and maximum frequency of the element are denoted by ω_{min} and ω_{max} , respectively, and the duration of the element is denoted by Δt in panel (a).

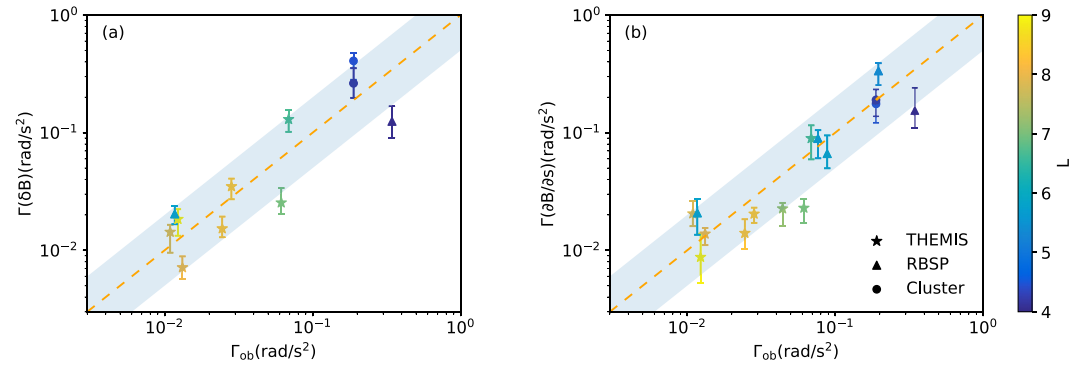


Figure 3. Comparisons between observational (Γ_{ob}) and theoretical chirping rates calculated with (a) Equation 4 $\Gamma(\delta B)$ and (b) Equation 6, $\Gamma(\delta B/\delta s)$. Different colors and markers categorize the L -shell value and data source of each case, respectively. The shadowed region is confined by lines $\Gamma = \Gamma_{\text{ob}}/2$ and $2\Gamma_{\text{ob}}$, while the orange dashed line denotes $\Gamma = \Gamma_{\text{ob}}$. Error bars indicate the range of Γ as pitch angle α varies from 65° to 75° ; the markers are calculated at exactly $\alpha = 70^\circ$.

chirping rates are less than a factor of two. The maximum difference for all events is less than a factor of three (not shown). Correspondingly, the direct comparison presented in Figure 3 demonstrates very good agreement between the new model and previously published observations. Furthermore, similar to chorus waves (Tao, Li, et al., 2012; Tao et al., 2014; Xie et al., 2021), we can see a decrease of chirping rate as L increases because of smaller magnetic field inhomogeneity at larger L -shells.

The discrepancies between observations and theoretical predictions come mainly from uncertainties in some parameters, such as wave amplitude (δB), the nonlinear parameter R , the pitch angle α , and source location (s_0). Although we select events with $|\text{MLAT}| < 5^\circ$ when calculating δB , the wave amplitude might still be different from its equatorial value, and the parameter R might take a value different from 0.5 (Tao et al., 2017; Teng et al., 2023). As an example, we show the uncertainty of theoretical chirping rates caused by varying the pitch angle α from 65° to 75° in Figure 3. Furthermore, the equation $s_0 = (2\pi|v_r|/\xi\Omega_{i0})^{1/3}$ we use to estimate the source location is only an estimation to the lowest order by assuming adiabatic motions of ions. To be exact, the release location needs to be calculated by taking full nonlinear wave particle interactions into consideration (Tao et al., 2021; Y. Wu et al., 2022). Other potential causes of estimation errors include the assumption of constant cold plasma density along the field line, and the fitting of $k(\omega)$. In general, taking these possible sources of uncertainties into consideration, we conclude that good agreement between observations and two different yet consistent theoretical chirping rate estimates has been reached. Therefore, the model proposed in Section 2 could well explain the chirping of EMIC waves in a different way from previous ones (Omura et al., 2010; Traktengerts & Demekhov, 2007).

4. Summary

In this work, we presented a new model of EMIC wave chirping and directly compared it with in situ satellite observations. The two theoretical predictions of chirping rates exhibit good agreement with observations, indicating that both rates are manifestations of the same underlying process at different stages of wave packet propagation. The new model not only relates EMIC wave chirping to wave amplitude at the equator but also to background magnetic field inhomogeneity, which is a novel contribution. The new chirping rate allows an easy explanation of the dependence of EMIC wave chirping rate on L -shell in the magnetosphere. Combining both predictions also opens up new possibilities. For example, we may estimate wave amplitude of rising-tone EMIC waves directly from the background magnetic field inhomogeneity (Z. Wu et al., 2023).

Furthermore, our comparison confirms that the principle of the TaRA model, initially developed for whistler mode chorus, is equally applicable to EMIC wave chirping. We note that some components of the TaRA model, such as phase-locking and detrapping, are also shared by Alfvén wave chirping in fusion plasmas from a recent study (X. Wang et al., 2022). Combining these findings suggests the possibility of a unified theoretical framework to explain the nonlinear chirping of different waves in various plasma environments (Chen & Zonca, 2016; Zonca et al., 2022).

Data Availability Statement

The electromagnetic field data used in this work are provided by Cluster, THEMIS, and Van Allen Probes satellites, and can be found at Z. An (2023).

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