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**Titolo**

Seismic risk computation for the fixed-base reactor building of the IRIS NPP

Ente emittente CIRTEN

## PAGINA DI GUARDIA

**Descrittori**

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**Sommario**

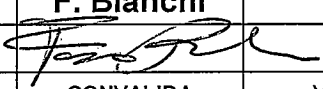
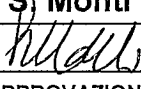
That report has been issued in the frame of the second research programme of ENEA-MSE agreement and it is one of the deliverables of the task I “Seismic analysis” of the work-programme 2 “Evolutionary INTD reactors” of the research theme on “Nuovo Nucleare da Fissione”.

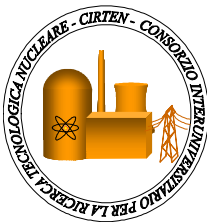
The report deals with the fragility assessment of the IRIS reactor building in its original configuration, i.e. without any isolation system. The assessment is based on the methodology developed by POLIMI in the 1<sup>st</sup> PAR (Piano Annuale di Realizzazione).

**Note**

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**CIRTEN**  
**CONSORZIO INTERUNIVERSITARIO**  
**PER LA RICERCA TECNOLOGICA NUCLEARE**

***POLITECNICO DI MILANO***  
**DIPARTIMENTO DI INGEGNERIA STRUTTURALE**  
**DIPARTIMENTO DI ENERGIA**

# ***SEISMIC RISK COMPUTATION FOR THE FIXED-BASE REACTOR BUILDING OF THE IRIS NPP***

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## **1. Introduction**

This report deals with the fragility assessment of the IRIS reactor building in its original configuration, i.e. without any isolation system: the aim of the fragility computation is the comparison between the performance of the traditional and the isolated building. The latter will be investigated in a following step.

The assessment is based on the procedure described in [1], on a finite element (FE) discretization and on repeated seismic analyses performed, via the ANSYS FE code [2], with the modal superposition technique.

The most important requirement of the procedure is to reduce as much as possible the uncertainties related to the incomplete knowledge and accuracy in defining models and methods; this reduction is here sought by refining analysis procedures and using consolidated analytical and numerical tools.

Secondly, the definition of the random variables is a key aspect of the analysis; the generation of the seismic excitations is the next requisite for setting up the assessment of the random vibration response of the structural system.

The computation of the exceedance probability is here performed via Monte Carlo simulation and First Order Reliability Method (FORM); to reduce the computational effort, the Response Surface (RS) method is used to express the seismic response as a function of the variation of the adopted random parameters.

The generation of the RSs is performed in terms of mean and standard deviation of the extreme value of an engineering parameter, such as the total acceleration at a given point or the AVerage floor Spectrum Acceleration (AVSA) over a frequency range.

Finally, the results of the fragility analysis are tested, also in view of a refinement of the response surfaces, within a complete risk assessment for a prototype site. The results are commented also in light of the problems associated to the hazard definition.

## 2. The FE structural model

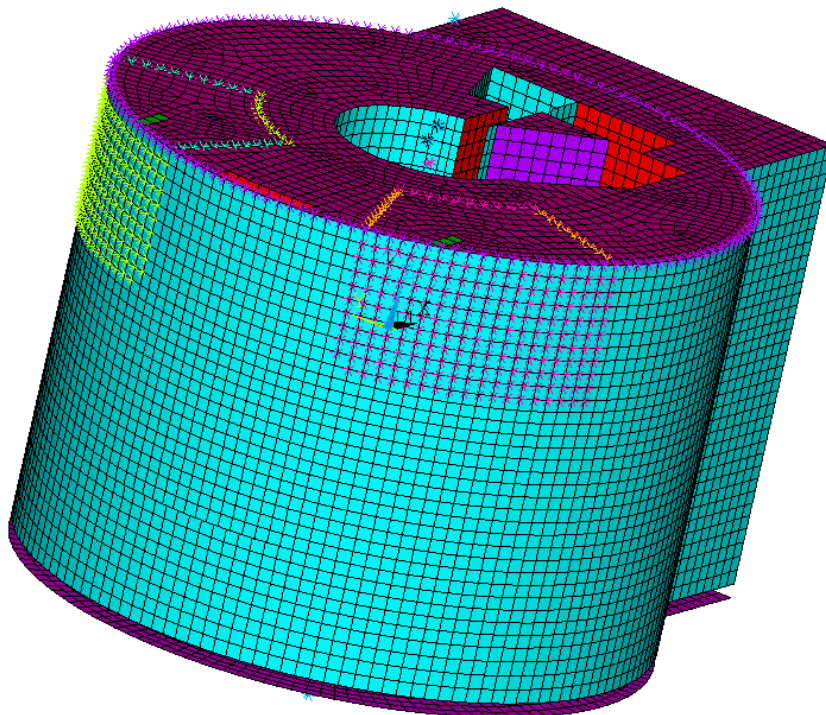
The structural model has been developed at Westinghouse EC [3] along with the procedures for running the numerical analyses and extrapolating the results.

The main characteristics of the whole numerical model are here briefly summarized:

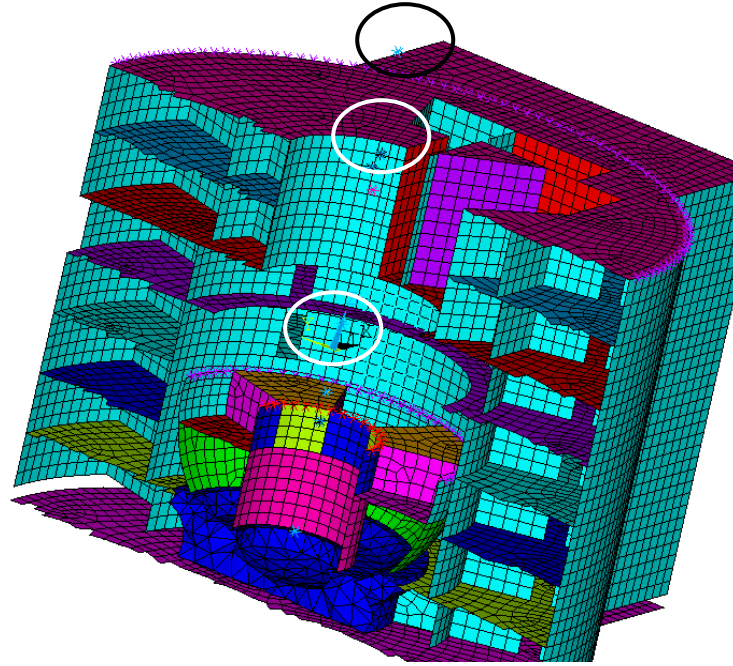
Nr. Key points . . . . .	.827
Nr. Lines . . . . .	.1620
Nr. Areas . . . . .	.804
Nr. Volumes . . . . .	.4
Nr. Nodes . . . . .	.29764
Nr. Elements. . . . .	.36382
Nr. Element types . . . . .	.47
Nr. Real constant sets. . . . .	.14017
Nr. Constraint equations. . . . .	.10992

Figure 1 reports on the FE whole model. Figure 2 and 3 describe the  $x=0$  and  $y=0$  sections, respectively. It is possible to observe the reinforced concrete (RC) walls and slabs modelled by 4-node shell elements and the base of the containment, which has been treated as a rigid body.

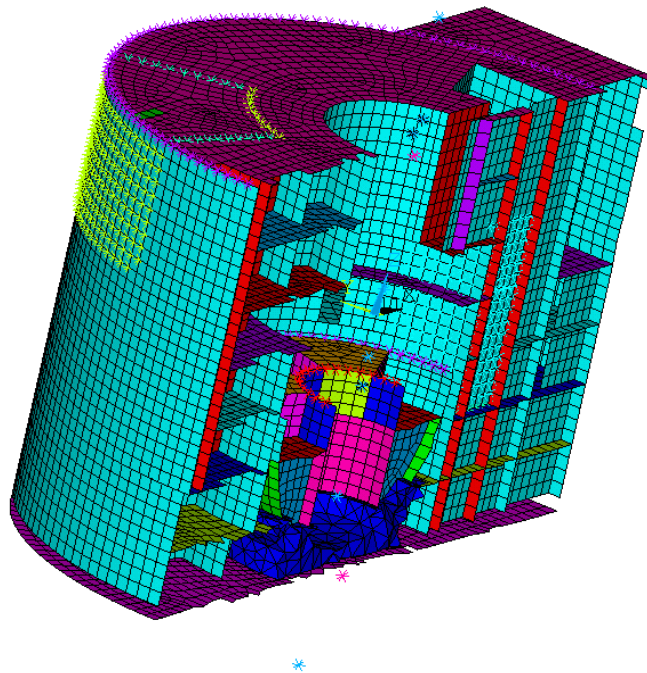
In particular in Figure 2 are underlined the positions of the concentrated masses (indicated by “\*”), which have been used for modelling, by an equivalent double-pendulum approach, the vessel, the containment and the roof of the reactor building.



**Figure 1.** The Finite Element model in ANSYS



**Figure 2.** FE model:  $x=0$  section



**Figure 3.** FE model:  $y=0$  section

### ***2.1 The vessel equivalent mechanical model***

Figure 4 reports the scheme of the structural vessel with its equivalent two-mass pendulum, called in the following equivalent mechanical model (EMM), with the main geometry characteristics.

The vessel EMM shall have the same following characteristics as the target structure, so to assure is interacts with the Auxiliary Building as the real component:

- total mass;
- position of centre of mass;
- moments of inertia about horizontal orthogonal axes through the centroid ;
- main eigenfrequencies.

Additional details can be found in [3].

By assuming that the vessel undergoes a rigid body motion with horizontal translation and rotation about horizontal axes, the following equivalence relations hold:

### **Plan XZ**

$$-Ma_{gx} = -m_1a_{1x} - m_2a_{2x} \quad (1)$$

$$-Ma_{gx}z_g - I_{gy}\ddot{\vartheta}_y = -m_1a_{1x}|h_1| + m_2a_{2x}|h_2| \quad (2)$$

$$a_{px} = a_{gx} + \ddot{\vartheta}_y z_p \quad (3)$$

### **Plan YZ**

$$-Ma_{gy} = -m_1a_{1y} - m_2a_{2y} \quad (4)$$

$$+Ma_{gy}z_g - I_{gx}\ddot{\vartheta}_x = +m_1a_{1y}|h_1| - m_2a_{2y}|h_2| \quad (5)$$

$$a_{py} = a_{gy} - \ddot{\vartheta}_x h_p \quad (6)$$

where

$h_p = 6.675$  m

$I_{gx} = I_{gy} = 76020000$  m<sup>4</sup>

$z_g = 0.525$  m

$h_1 = 2.2$  m,  $h_2 = 20.9$  m

$m_1 = 1955200$  kg,  $m_2 = 152853$  kg

$M = m_1 + m_2$ ,

$\ddot{\vartheta}$

$a_1, a_2, a_g, a_p$

is the level of the reactor coolant pumps (RCP) with respect to the concrete surface supporting the vessel,

is the vessel inertia moment,

is the level of the vessel centroid,

are the levels of the masses,

are the concentrated masses of the EMM,

is the total mass of the vessel,

is the angular acceleration of the vessel,

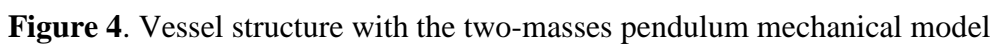
are the accelerations at mass 1, mass 2, vessel centroid and RCP level.

The previous equations can be used to estimate the horizontal acceleration and rotational acceleration of the vessel, under the hypothesis that deformations are concentrated at the level of the supports. By this strategy it is possible to evaluate the horizontal acceleration (in  $x$  and  $y$  direction) at any level inside the vessel (e.g. the RCP level) starting from the FE calculated accelerations of the two concentrated masses  $m_1$  and  $m_2$ .

## ***2.2 The soil structure interaction simplified model***

Soil structure interaction (SSI) can be identified as the aspect that most highly affects the response of the auxiliary building. It represents the coupling of the structure with the soil under its foundation during a seismic excitation. A seismic response during an earthquake will depend not only on the properties of the structure itself but also on the properties of the soil around and of the excitation signal. This phenomenon, called dynamic interaction, becomes more important the higher is the

The soil-structure interaction is here simulated by spring and dashpot elements which connect the FE reactor building to the reference system in  $x$ ,  $y$  and  $z$  directions. The properties of these elements have been defined on the basis of the “quasi-rigid foundation” hypothesis, stating that the foundation mat can be regarded as a deformable body within the structural model, but essentially behaves as rigid when the interaction with the soil is considered [4]. Under this hypothesis the spring and dashpots distributed below the foundation model match, in terms of resultants, the total stiffness and damping parameters for the six DOFs (degrees of freedom) of the rigid model [5].



## 6

Four random variables have been here selected to represent the main sources of randomness (apart from the seismic excitation) for the computation of the response of an equipment located inside the vessel.

- $x_1$ : a random variable (lognormal distribution) describing the soil shear modulus  $G_s$ , with mean value of 100MPa and c.o.v. equal to 0.3;
- $x_2$ : a random variable (lognormal distribution) describing the soil damping factor  $\nu_s$ , with mean value of 20% and c.o.v. equal to 0.3;
- $x_3$ : a random variable (lognormal distribution) describing the concrete elastic modulus  $E_c$ , with mean value of 21000MPa and c.o.v. equal to 0.22;
- $x_4$ : a random variable (lognormal distribution) describing the concrete damping factor  $\nu_c$ , with mean value of 5% and c.o.v. equal to 0.22;

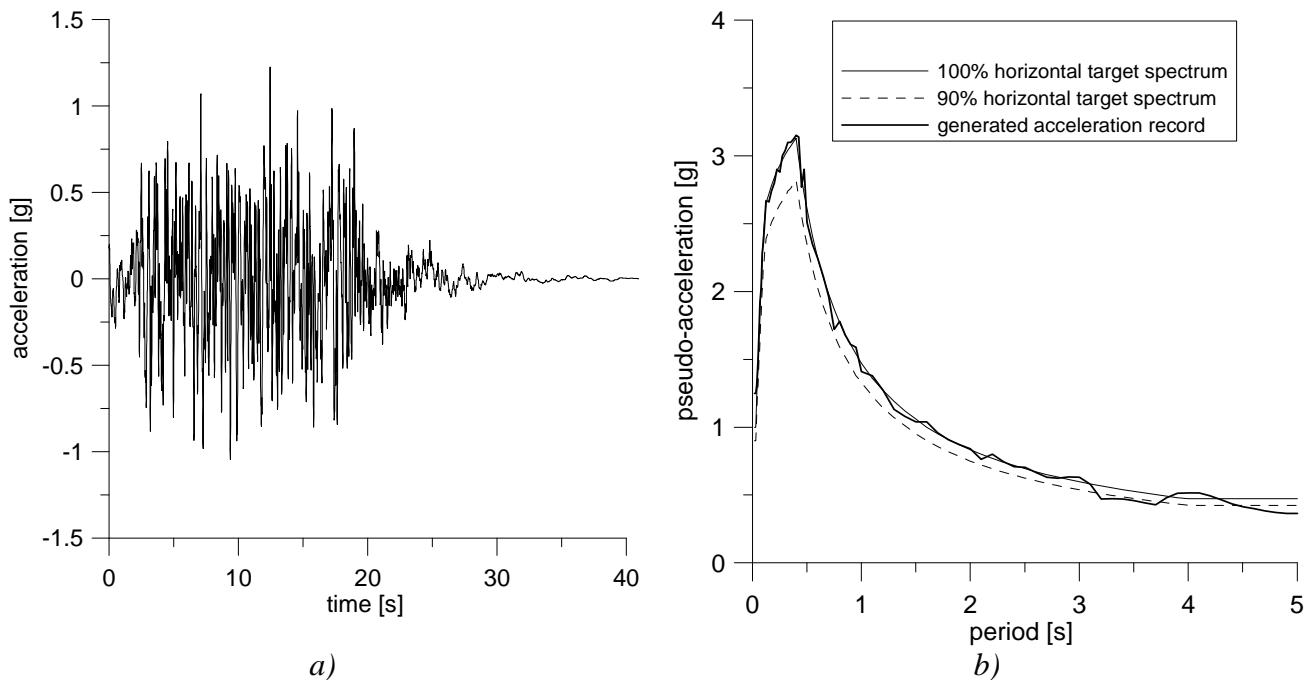
The soil stiffness and damping are introduced by springs and dashpots as in Figure 3. The concrete damping is introduced in the ANSYS FE code by the material-dependent coefficient for stiffness proportional viscous damping. This is related to the damping coefficient  $\nu$  through the relation

$$\beta = \frac{2\nu}{\omega} \quad (7)$$

where  $\omega$  is the circular frequency associated to the structure mode shape which mainly characterize the deformation of the concrete elements.

#### 4. The seismic excitation

The Response Spectra prescribed by the USNRC 1.60 (1973) [6] was adopted as seismic input. The spectral parameters were treated as deterministic, so that a single set of 20 input motions, each described by three components, has been generated and used at all experimental points. Generation was performed starting from white-noise accelerograms, modulated in the time domain, and iteratively correcting their Fourier Amplitude Spectra in order to match the USNRC 1.60 (1973) curve. An example of the accelerograms obtained is given in Figure 5.



**Figure 5.** Example of an artificial accelerogram with the target spectra from USNRC 1.60 (1973) – damping 5%.

The set of 20 input motions have been prepared by this procedure for being applied to the follow probabilistic assessment.

## 5. Design of experiments: Central Composite Design

For representing the reactor building response a second-order model can be used in the application of the Response Surface Method to the structural problem [1]. A full model (i.e. encompassing all quadratic terms) requires, for  $k$  random variables, the estimation of  $p=1+k+k(k+1)/2$  coefficients. In this situation the most suitable experimental strategy is the “Central Composite Design” (CCD); once fixed a “center point”, CCD is the combination of a classical “two-level factorial design”, in which all the combinations of two levels (high/low) of the random variables are considered, with a “star design”. In the latter  $2k$  points are considered in which one variable takes an intermediate value and the others are at the central value. Including the central point, a total number of experiments equal to  $n=2^k+2k+1$  is reached. Reasoning in terms of non-dimensional zero-mean random variables  $\eta_i = (x_i - \mu_{xi}) / \sigma_{xi}$  while for preserving the “rotatability” of the design the star points must be placed at  $\alpha = \eta_i = \sqrt[4]{2^k}$ . In this study for  $k=4$ , it results  $p=15$ ,  $n=25$  and  $\alpha = 2$ .

Table I summarizes the design of experiments (DoE) for the selected random variables, normalized to the mean value.

**Table I.** DoE with mean value normalization

$G_s$	$v_s$	$v_c$	$E_c$
1	0.4	1	1
1.9	0.483	0.588	1.616666667
1.9	0.483	0.588	0.588
0.485	0.483	0.588	1.616666667
0.485	0.483	0.588	0.588
0.485	0.483	1.62	0.588
1.9	0.483	1.62	1.616666667
0.485	0.483	1.62	1.616666667
1.9	0.483	1.62	0.588
1	1	1	1
1.6	1	1	1
1	1	1	1.44
1	1	1	0.56
1	1	0.56	1
0.4	1	1	1
1	1	1.44	1
1	1.6	1	1
1.9	1.9	0.588	1.616666667
1.9	1.9	0.588	0.588
0.485	1.9	0.588	1.616666667
0.485	1.9	0.588	0.588
0.485	1.9	1.62	0.588
1.9	1.9	1.62	1.616666667

0.485	1.9	1.62	1.616666667
1.9	1.9	1.62	0.588

## 6. Influence of the vessel damping in the structural response

In the selection of the random variables the vessel damping has been initially taken into consideration. However, from previous analyses on an equivalent case study was shown how its variability does not contribute significantly to the structural response, in term of the selected engineering parameter (the acceleration at the RCP level), so it can be neglected [1].

As a verification, during the preliminary investigations, a structural analysis on 20 simulated seismic accelerations has been performed. Table II reports the results in terms of mean value ( $\bar{a}_{RCP}$ ) and standard deviation ( $\sigma_{a_{RCP}}$ ) of the extreme acceleration computed at the RCP level. It is possible to see how varying only the vessel damping and maintaining constant at their mean values the remain parameters, the statistical response does not show reasonable variations.

In light of these considerations, the vessel damping has not been considered as a structural variable provided with a significant randomness.

**Table II.** DoE with mean value normalization

$G_s$	$v_s$	$v_v$ vessel damping	$v_c$	$E_c$	$\bar{a}_{RCP}$	$\sigma_{a_{RCP}}$
1	1	0.588	1	1	1.961706	0.1458248
1	1	1.62	1	1	1.958110	0.1467642
1	1	1	1	1	1.957478	0.1479528

**Table III.** Extreme absolute acceleration at the RCP level

$G_s$	$v_s$	$v_c$	$E_c$	$\bar{a}_{RCP}$	$\sigma_{a_{RCP}}$
1	0.4	1	1	2.781052	0.181732
1.9	0.483	0.588	1.616666667	3.149629	0.191692
1.9	0.483	0.588	0.588	3.45202	0.369668
0.485	0.483	0.588	1.616666667	1.973489	0.155873
0.485	0.483	0.588	0.588	2.023667	0.138723
0.485	0.483	1.62	0.588	2.002153	0.133574
1.9	0.483	1.62	1.616666667	3.093401	0.184469
0.485	0.483	1.62	1.616666667	1.968522	0.15441
1.9	0.483	1.62	0.588	3.265414	0.361528
1	1	1	1	1.957478	0.147953
1.6	1	1	1	2.532745	0.212191
1	1	1	1.44	1.941101	0.142368
1	1	1	0.56	2.017759	0.192984
1	1	0.56	1	1.978061	0.14357
0.4	1	1	1	1.223987	0.101341

1	1	1.44	1	1.948665	0.146817
1	1.6	1	1	1.696085	0.141293
1.9	1.9	0.588	1.616666667	1.829047	0.116976
1.9	1.9	0.588	0.588	2.157065	0.180767
0.485	1.9	0.588	1.616666667	1.239875	0.11683
0.485	1.9	0.588	0.588	1.375786	0.130622
0.485	1.9	1.62	0.588	1.323353	0.126866
1.9	1.9	1.62	1.616666667	1.807637	0.117073
0.485	1.9	1.62	1.616666667	1.231432	0.118063
1.9	1.9	1.62	0.588	2.035637	0.161702

## 7. Application of the response surface method

Running the experiments detailed in Table I, once fixed the seismic input spectral parameters, it is possible to compute the extreme structural response at the RCP level in terms mean and standard deviation of the absolute acceleration in the horizontal plane (the acceleration vector intensity in the horizontal plane as computed with  $x$  and  $y$  components). Table III reports the 25 experiments for the central composite design and the computation of the Response Surface. The soil shear modulus modifies with more emphasis the structural response. In Appendix A are reported the absolute acceleration response time histories at the RCP and vessel supports level for three type of soil shear modulus  $G_s$  maintaining constant the remaining ones at their mean values.

**Table IV. AVSA 1-2Hz**

$G_s$	$v_s$	$v_c$	$E_c$	$\bar{A}_{RCP}$	$\sigma_{A_{RCP}}$
1	0.4	1	1	7.307136	0.530469
1.9	0.483	0.588	1.616666667	3.786385	0.120859
1.9	0.483	0.588	0.588	4.31388	0.168213
0.485	0.483	0.588	1.616666667	7.77025	0.436987
0.485	0.483	0.588	0.588	7.754443	0.487412
0.485	0.483	1.62	0.588	7.711118	0.479911
1.9	0.483	1.62	1.616666667	3.773081	0.120654
0.485	0.483	1.62	1.616666667	7.747669	0.433481
1.9	0.483	1.62	0.588	4.265076	0.159607
1	1	1	1	5.377814	0.215423
1.6	1	1	1	4.116661	0.13216
1	1	1	1.44	5.213352	0.195495
1	1	1	0.56	5.701189	0.263837
1	1	0.56	1	5.38647	0.216207
0.4	1	1	1	4.30029	0.212365
1	1	1.44	1	5.369208	0.214603
1	1.6	1	1	4.558221	0.173455
1.9	1.9	0.588	1.616666667	3.336638	0.091932
1.9	1.9	0.588	0.588	3.616884	0.116232
0.485	1.9	0.588	1.616666667	4.254613	0.20566
0.485	1.9	0.588	0.588	4.233076	0.207751
0.485	1.9	1.62	0.588	4.224263	0.206741
1.9	1.9	1.62	1.616666667	3.334459	0.091488
0.485	1.9	1.62	1.616666667	4.249733	0.205074

1.9	1.9	1.62	0.588	3.608512	0.114904
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The adoption of the so called “dual response surface” approach for solving the reliability problem under stochastic input is considered. The analytical expression of the response surface has the following form for both the mean surface and the standard deviation surface:

$$g(\underline{x}) = a_0 + a_1x_1 + a_2x_2 + a_3x_3 + a_4x_4 + a_5x_1x_2 + a_6x_1x_3 + a_7x_1x_4 + a_8x_2x_3 + a_9x_2x_4 + a_{10}x_3x_4 + a_{11}x_1^2 + a_{12}x_2^2 + a_{13}x_3^2 + a_{14}x_4^2 \quad (8)$$

The RS computation involves not only the horizontal absolute acceleration but also the averaged floor spectrum acceleration in two frequency intervals (AVSA), 1-2Hz and 2-5Hz (AVSA 1-2Hz and AVSA 2-5Hz respectively). In other words, an acceleration spectrum 3% damped is computed for all the experiments acceleration time history output in horizontal  $x$  and  $y$  direction, for each of the 20 time history samples. Only the maximum value between  $x$  and  $y$  is then considered for each one 1-2Hz and 2-5Hz intervals. Finally the mean value and the standard deviation value over 20 time histories is evaluated for each design point. Table IV and V reports the extreme values  $A_{RCP}$  and standard deviation  $\sigma_{A_{RCP}}$  in terms of AVSA at the experimental points.

**Table V.** AVSA 2-5Hz

$G_s$	$v_s$	$v_c$	$E_c$	$\bar{A}_{RCP}$	$\sigma_{A_{RCP}}$
1	0.4	1	1	8.481598	0.385064
1.9	0.483	0.588	1.616666667	11.93782	0.619822
1.9	0.483	0.588	0.588	11.93558	0.813467
0.485	0.483	0.588	1.616666667	3.155568	0.075547
0.485	0.483	0.588	0.588	3.170652	0.116668
0.485	0.483	1.62	0.588	3.156497	0.112947
1.9	0.483	1.62	1.616666667	11.743	0.58766
0.485	0.483	1.62	1.616666667	3.148128	0.074806
1.9	0.483	1.62	0.588	11.46948	0.707226
1	1	1	1	5.500332	0.18179
1.6	1	1	1	9.084592	0.396367
1	1	1	1.44	5.782434	0.184431
1	1	1	0.56	4.879084	0.133936
1	1	0.56	1	5.513599	0.18267
0.4	1	1	1	2.063821	0.052879
1	1	1.44	1	5.488494	0.180722
1	1.6	1	1	4.508377	0.117353
1.9	1.9	0.588	1.616666667	6.373285	0.218086
1.9	1.9	0.588	0.588	6.238751	0.205447
0.485	1.9	0.588	1.616666667	2.400567	0.051564
0.485	1.9	0.588	0.588	2.247113	0.049067
0.485	1.9	1.62	0.588	2.251127	0.048952
1.9	1.9	1.62	1.616666667	6.342643	0.214682
0.485	1.9	1.62	1.616666667	2.401576	0.051491
1.9	1.9	1.62	0.588	6.15621	0.201247

In light of these considerations the six RSs , function of four random variables, have been processed by an ordinary least squares method and the following  $a_{0-14}$  parameters result.

RCP absolute acceleration (MEAN)

$a_0=1.986767707$ ;  
 $a_1=2.261109248$ ;  
 $a_2=-2.059244968$ ;  
 $a_3=1.19E-02$ ;  
 $a_4=-4.38E-02$ ;  
 $a_5=-0.422690008$ ;  
 $a_6=-0.297249737$ ;  
 $a_7=-5.74E-02$ ;  
 $a_8=-0.130951806$ ;  
 $a_9=0.734595069$ ;  
 $a_{10}=1.00E-02$ ;  
 $a_{11}=-4.11E-02$ ;  
 $a_{12}=-3.80E-02$ ;  
 $a_{13}=6.62E-02$ ;  
 $a_{14}=8.07E-03$ ;

RCP absolute acceleration (STANDARD DEVIATION)

$a_0=0.153058732$ ;  
 $a_1=0.219873571$ ;  
 $a_2=-5.16E-02$ ;  
 $a_3=5.69E-02$ ;  
 $a_4=-0.187734841$ ;  
 $a_5=-1.61E-04$ ;  
 $a_6=-5.62E-02$ ;  
 $a_7=-5.05E-03$ ;  
 $a_8=-8.30E-02$ ;  
 $a_9=1.34E-02$ ;  
 $a_{10}=-6.40E-04$ ;  
 $a_{11}=3.11E-02$ ;  
 $a_{12}=-2.82E-02$ ;  
 $a_{13}=6.48E-03$ ;  
 $a_{14}=8.56E-02$ ;

AVSA 1-2Hz (MEAN)

$a_0=12.08381275$ ;  
 $a_1=4.360644212$ ;  
 $a_2=-8.066750513$ ;  
 $a_3=-2.377333182$ ;  
 $a_4=-3.808669312$ ;  
 $a_5=-3.044135739$ ;  
 $a_6=1.445149064$ ;  
 $a_7=-2.33E-02$ ;  
 $a_8=-0.302780408$ ;  
 $a_9=2.033693858$ ;  
 $a_{10}=2.71E-03$ ;  
 $a_{11}=7.28E-02$ ;

$a_{12}=1.084985892$ ;  
 $a_{13}=39.06E-03$ ;  
 $a_{14}=1.765669193$ ;

#### AVSA 1-2Hz (STANDARD DEVIATION)

$a_0=0.839138718$ ;  
 $a_1=0.203965487$ ;  
 $a_2=-1.120557626$ ;  
 $a_3=0.172724883$ ;  
 $a_4=-9.28E-02$ ;  
 $a_5=-0.198212087$ ;  
 $a_6=0.107294605$ ;  
 $a_7=9.87E-05$ ;  
 $a_8=-5.12E-03$ ;  
 $a_9=0.358419583$ ;  
 $a_{10}=4.45E-03$ ;  
 $a_{11}=2.51E-02$ ;  
 $a_{12}=-8.52E-02$ ;  
 $a_{13}=5.17E-03$ ;  
 $a_{14}=1.41E-02$ ;

#### AVSA 2-5Hz (MEAN)

$a_0=-2.467263779$ ;  
 $a_1=10.03382239$ ;  
 $a_2=-5.666644261$ ;  
 $a_3=2.697221384$ ;  
 $a_4=5.998668132$ ;  
 $a_5=-1.113923658$ ;  
 $a_6=-2.323411686$ ;  
 $a_7=-0.139826832$ ;  
 $a_8=2.56E-02$ ;  
 $a_9=2.495470841$ ;  
 $a_{10}=0.122579963$ ;  
 $a_{11}=6.95E-02$ ;  
 $a_{12}=-1.299132153$ ;  
 $a_{13}=7.12E-02$ ;  
 $a_{14}=-2.745527477$ ;

#### AVSA 2-5Hz (STANDARD DEVIATION)

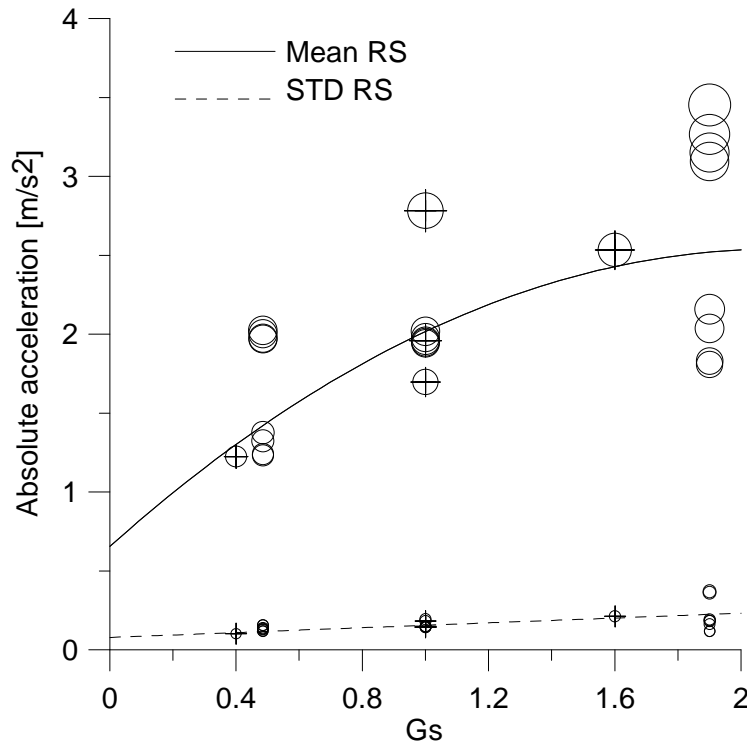
$a_0=-5.07E-02$ ;  
 $a_1=0.385736192$ ;  
 $a_2=-0.443144087$ ;  
 $a_3=8.77E-02$ ;  
 $a_4=0.40422987$ ;  
 $a_5=8.51E-02$ ;  
 $a_6=-0.213270791$ ;  
 $a_7=-2.47E-02$ ;  
 $a_8=-3.89E-02$ ;  
 $a_9=0.172529498$ ;  
 $a_{10}=2.31E-02$ ;

$a_{11}=7.08\text{E-}02$ ;  
 $a_{12}=-5.49\text{E-}02$ ;  
 $a_{13}=1.61\text{E-}02$ ;  
 $a_{14}=-0.226138886$ ;

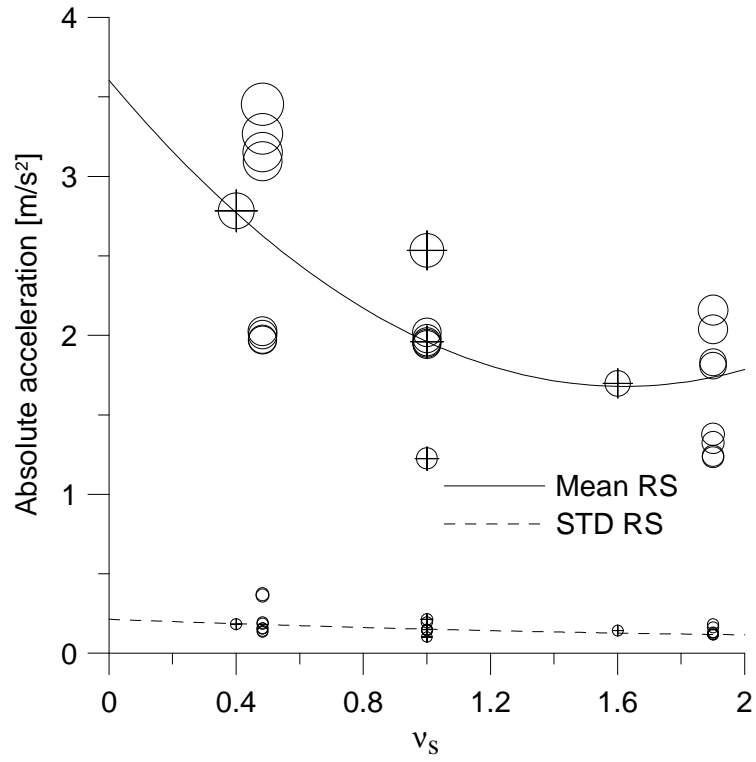
Figures 6-9 depict the main sections of the RSs in terms of both mean and standard deviation for the absolute acceleration at the RCP level. They are computed maintaining constant respectively  $x_2-x_3-x_4=1$ ,  $x_1-x_3-x_4=1$ ,  $x_1-x_2-x_4=1$ ,  $x_1-x_2-x_3=1$ . It is worth noting that the acceleration variability is more evident with the variation of the soil characteristics. The concrete properties variability seems to stress less the maximum acceleration response at the RCP level. This behavior emphasizes how the site characteristics can modify the structural response. The “+” symbols and “O” symbols in the figures reflect the experimental points on the same section and the remaining experimental points respectively.

Figure 10-13 reports the RSs processed maintaining constant respectively  $x_3-x_4=1$ ,  $x_1-x_2=1$ .

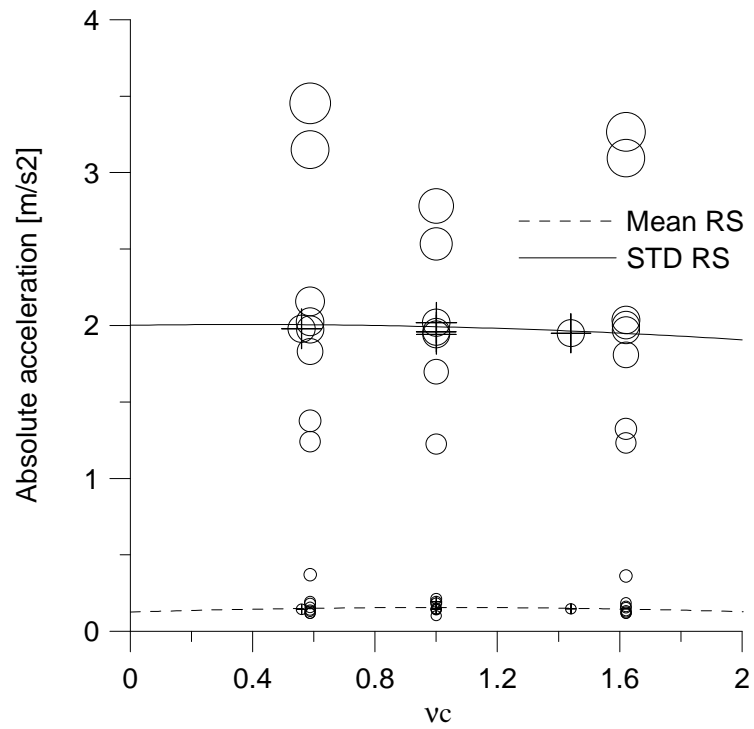
Figure 14-21 depict the RSs for AVSA 1-2Hz and 2-5Hz.



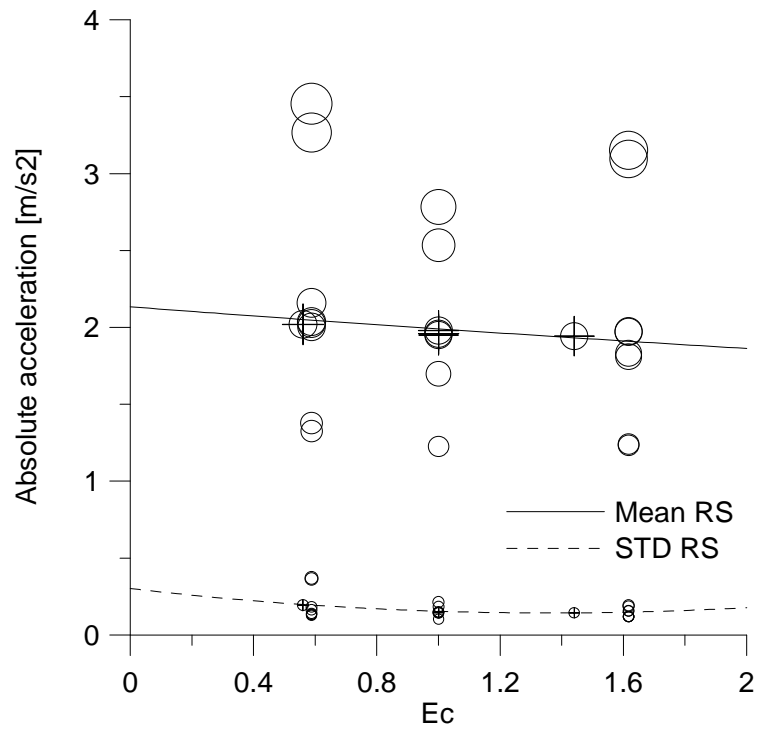
**Figure 6.** Absolute acceleration RS: section  $x_2=x_3=x_4=1$



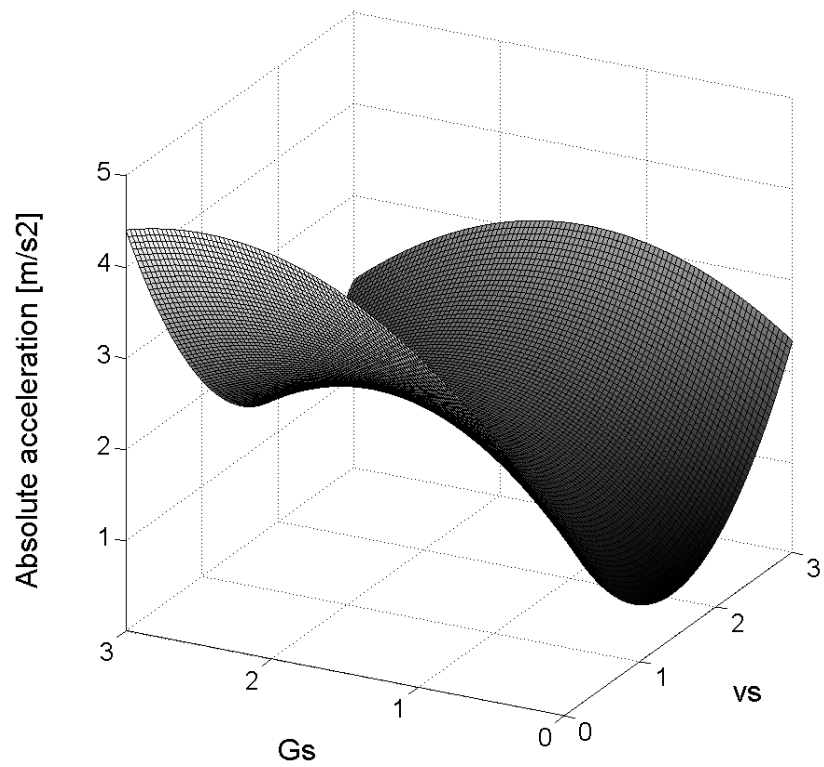
**Figure 7.** Absolute acceleration RS: section  $x_1=x_3=x_4=1$



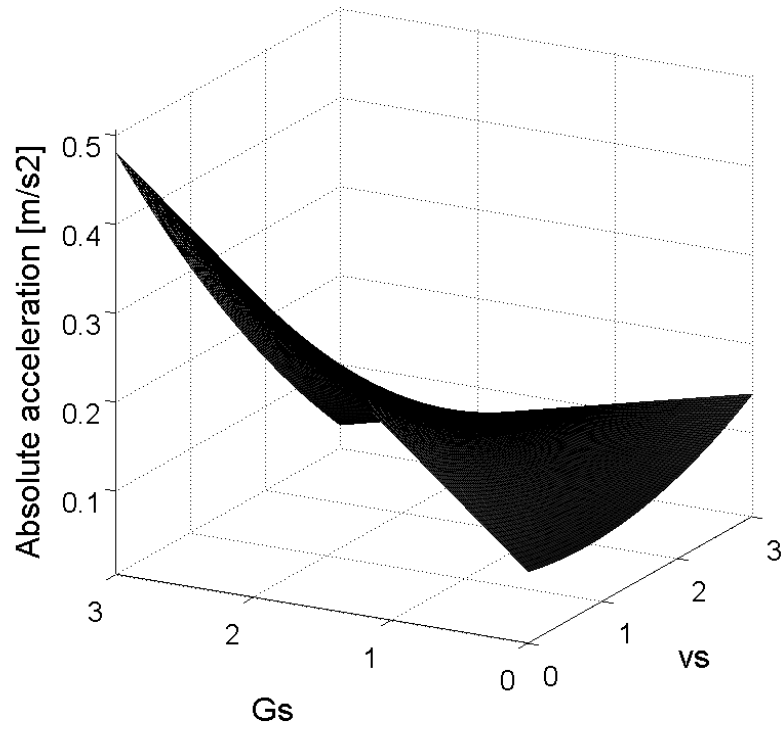
**Figure 8.** Absolute acceleration RS: section  $x_1=x_2=x_4=1$



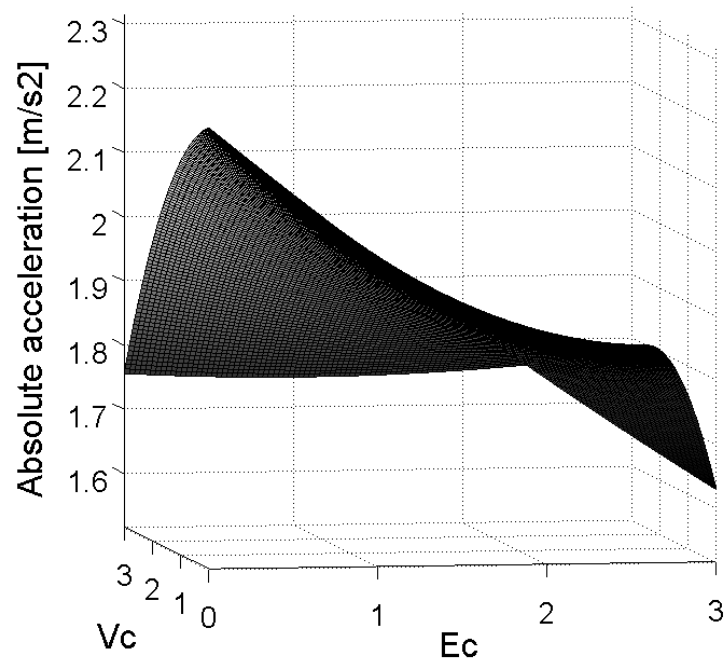
**Figure 9.** Absolute acceleration RS: section  $x_1=x_2=x_3=1$



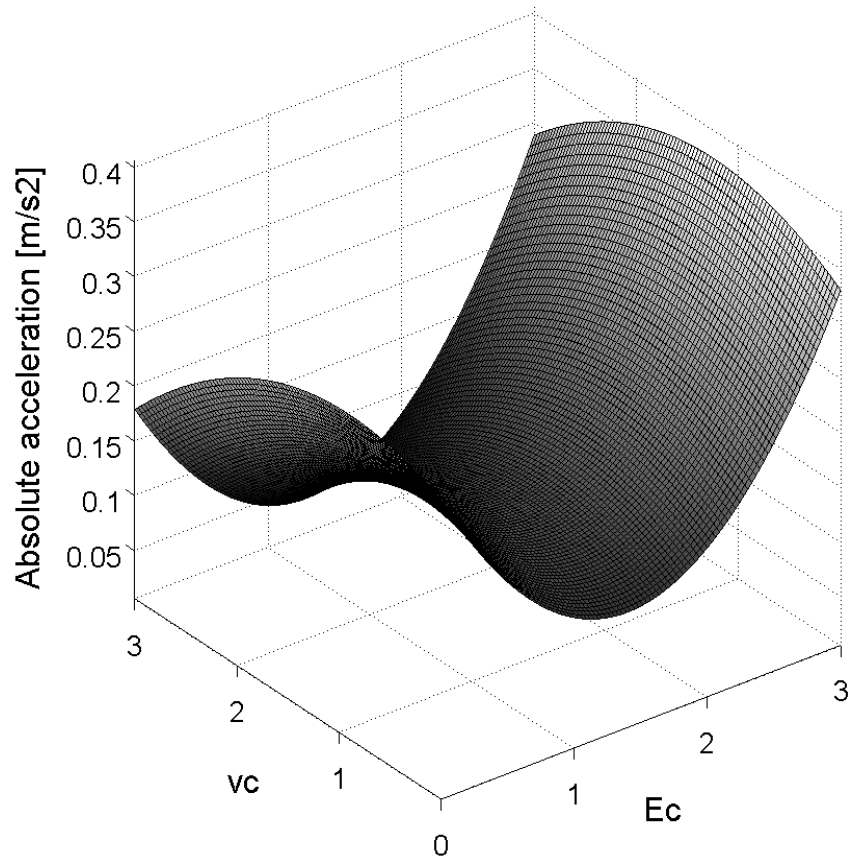
**Figure 10.** Absolute acceleration RS: surface “MEAN”  $x_3=x_4=1$



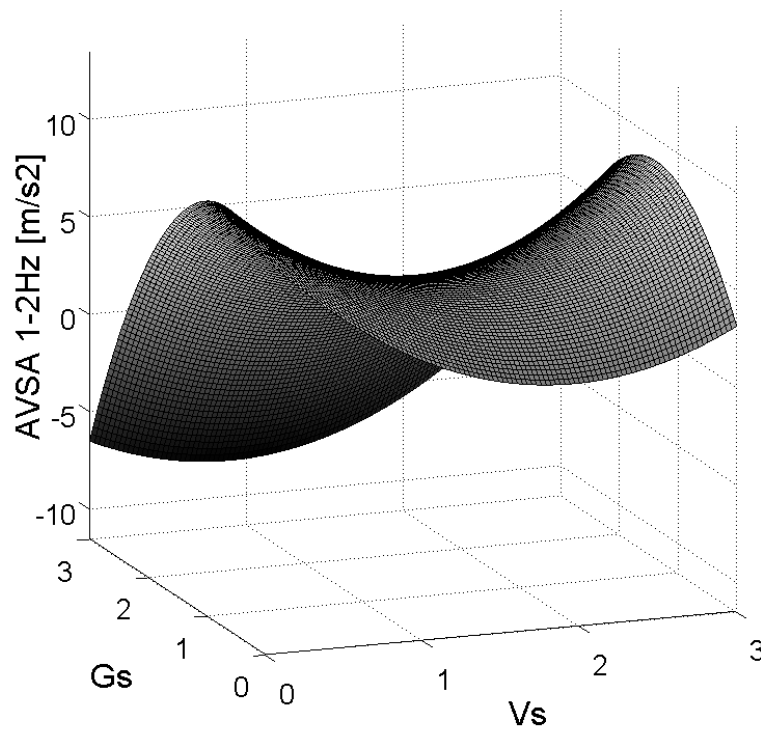
**Figure 11.** Absolute acceleration RS: surface “STD”  $x_3=x_4=1$



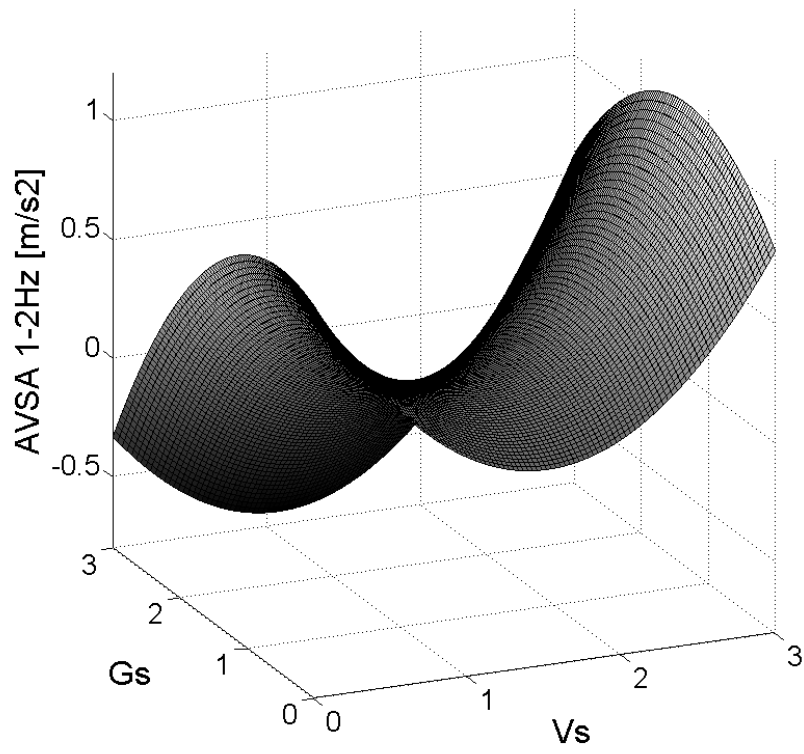
**Figure 12.** Absolute acceleration RS: surface “MEAN”  $x_1=x_2=1$



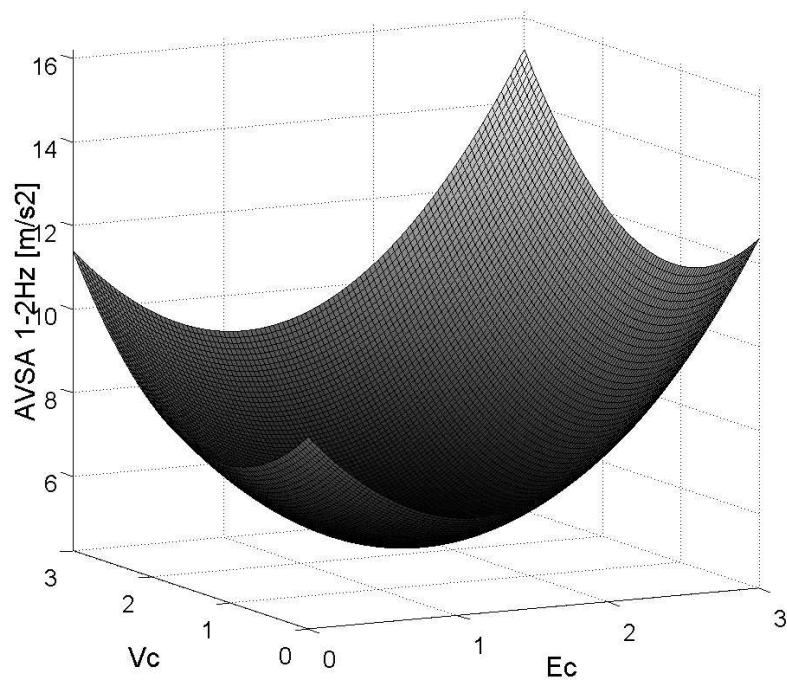
**Figure 13.** Absolute acceleration RS: surface “STD”  $x_1=x_2=1$



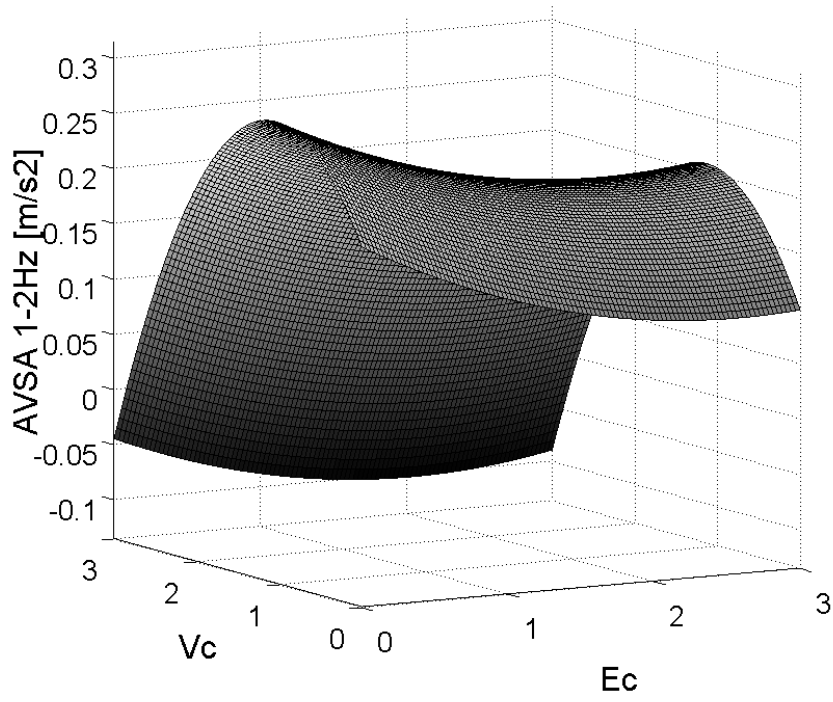
**Figure 14.** AVSA 1-2Hz RS: surface “MEAN”  $x_3=x_4=1$



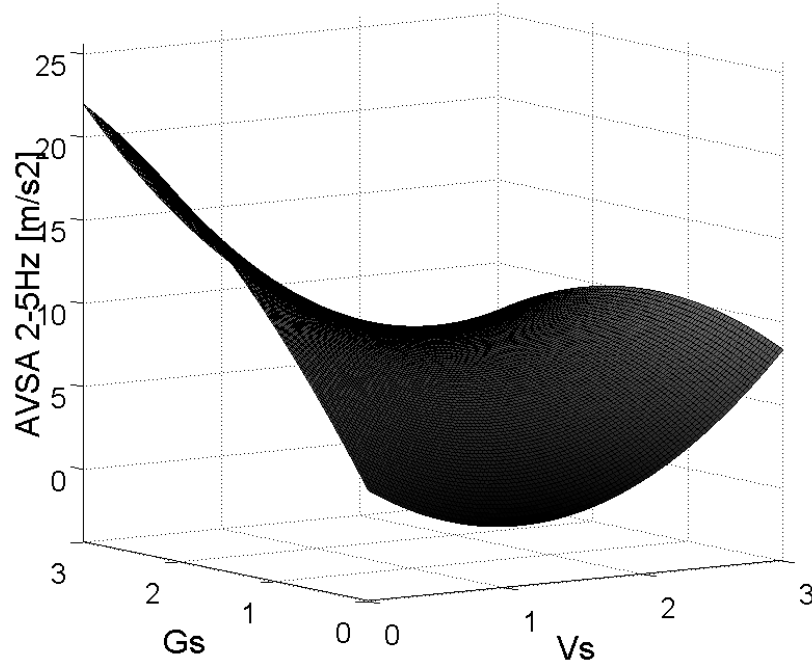
**Figure 15.** AVSA 1-2Hz RS: surface “STD”  $x_3=x_4=1$



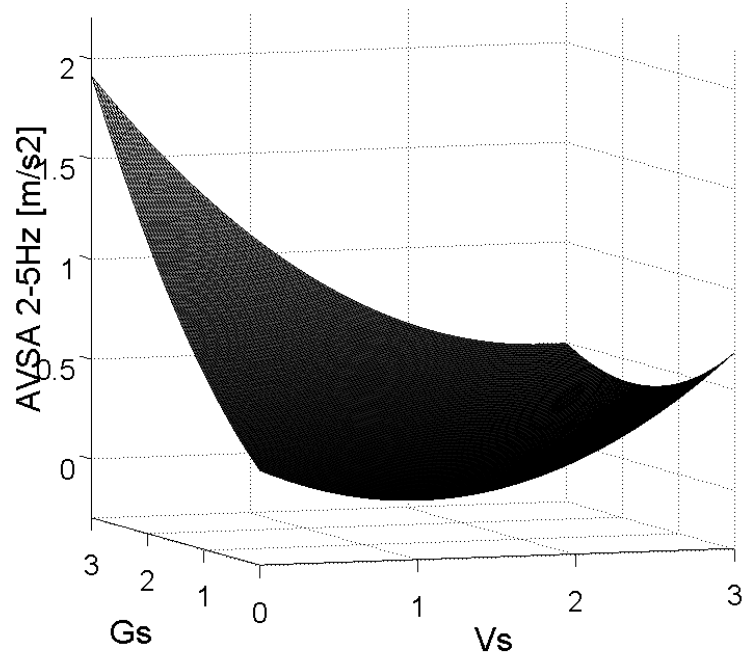
**Figure 16.** AVSA 1-2Hz RS: surface “MEAN”  $x_1=x_2=1$



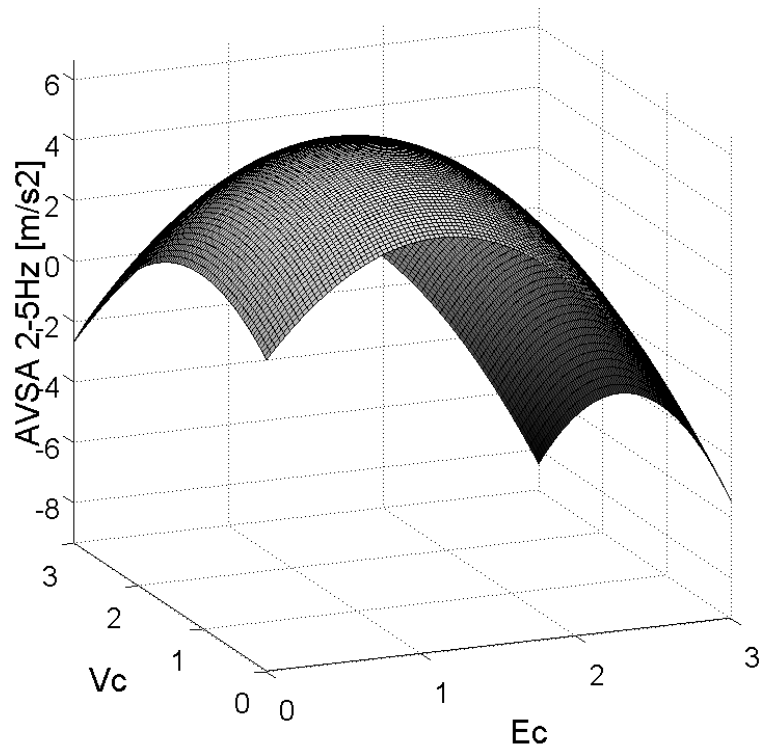
**Figure 17.** AVSA 1-2Hz RS: surface “STD”  $x_1=x_2=1$



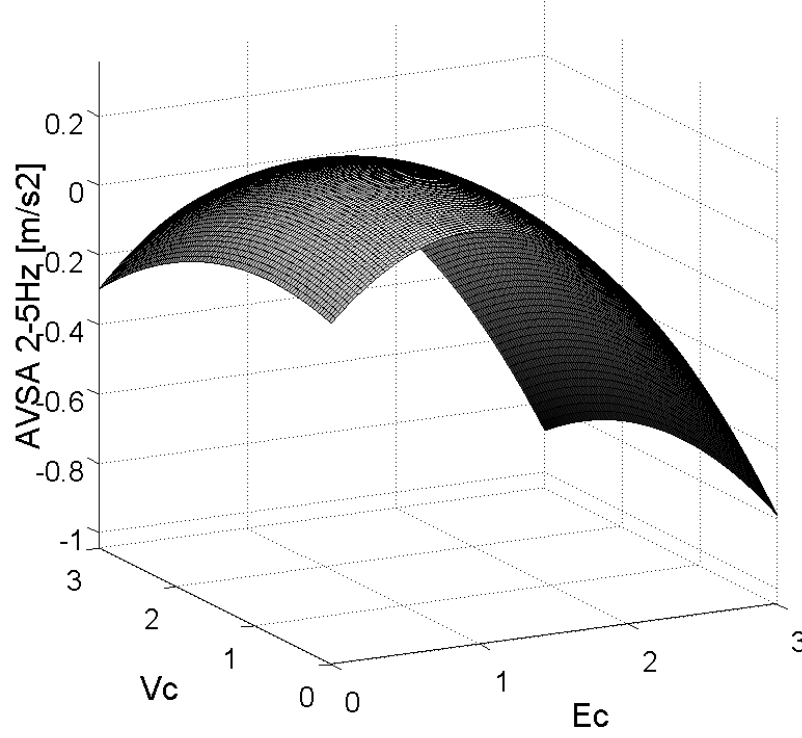
**Figure 18.** AVSA 2-5Hz RS: surface “MEAN”  $x_3=x_4=1$



**Figure 19.** AVSA 2-5Hz RS: surface “STD”  $x_3=x_4=1$



**Figure 20.** AVSA 2-5Hz RS: surface “MEAN”  $x_1=x_2=1$



**Figure 21.** AVSA 2-5Hz RS: surface “STD”  $x_1=x_2=1$

## 8. Fragility analysis

The fragility functions have been computed by the “hit or miss” Monte Carlo Method (MCM) and a First Order Reliability Method (FORM) [1, 7-9].

The RS supports the computational procedures. In particular the application of the MCM consists in a sequential generation of samples of lognormal variables ( $x_1 x_2 x_3 x_4$ ).

Taking into account the probabilistic parameters of a lognormally distributed random variable, one can evaluate the parameters of the variable’s natural logarithm (by definition, the variable’s logarithm is normally distributed) as

$$\bar{a} = \ln( M( X ) ) + 0.5 \ln \left( 1 + \frac{\Sigma( X )}{M( X )^2} \right) \quad (9)$$

$$\sigma^2 = \ln \left( 1 + \frac{\Sigma( X )}{M( X )^2} \right) \quad (10)$$

where  $\bar{a}$  and  $\sigma$  are the mean and standard deviation of the variable’s natural logarithm. Table VI reports the main normalized random variables statistic parameters where  $X$  is a random variable with a lognormal distribution, then  $Y = \ln(X)$  has a normal distribution.

For each sample extracted by the lognormal distributions it is possible to evaluate, by the mean and standard deviation response surfaces, the probability density function of the structural response in terms of extreme values of absolute acceleration, AVSA 1-2Hz and AVSA 2-5Hz.

The mean and standard deviation computed via the RSs, in fact, are subsequently used for extracting the acceleration demand from the Gumbel distribution for the extreme value; the

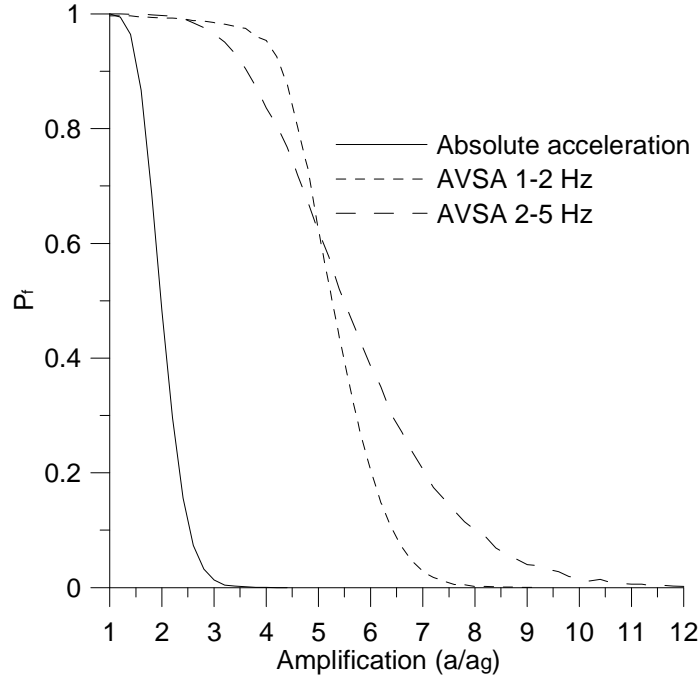
extracted value is compared to the critical threshold. By this procedure the exceedance probability is evaluated and the MCM fragility curve is completed.

**Table VI.** Normalized random variables statistic parameters

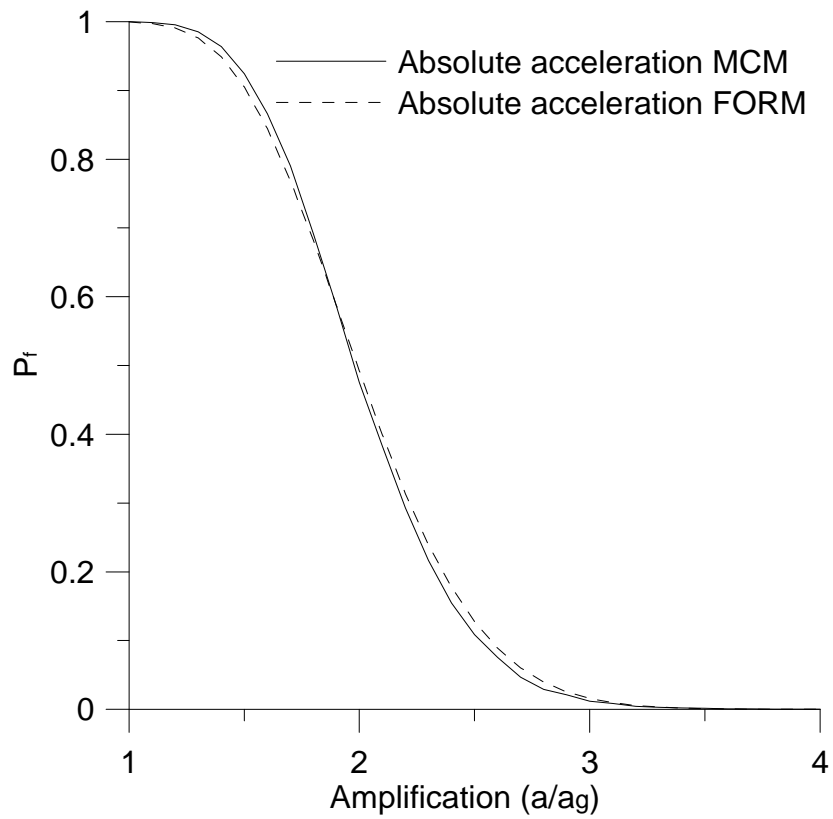
	Lognormal	Normal
$G_s$	$M(X)=1$	$\bar{a} = -0.04309$
	$\Sigma(X)=0.3$	$\sigma = 0.29356$
		$\sigma^2 = 0.086178$
$v_s$	$M(X)=1$	$\bar{a} = -0.04309$
	$\Sigma(X)=0.3$	$\sigma = 0.29356$
		$\sigma^2 = 0.086178$
$v_c$	$M(X)=1$	$\bar{a} = -0.02363$
	$\Sigma(X)=0.22$	$\sigma = 0.217406$
		$\sigma^2 = 0.047265$
$E_c$	$M(X)=1$	$\bar{a} = -0.02363$
	$\Sigma(X)=0.22$	$\sigma = 0.217406$
		$\sigma^2 = 0.047265$

Figure 22 depicts three fragility functions processed by MCM. The fragility is represented as the probability of exceeding the amplification  $a_{RCP} / a_g$  or  $AVSA_{RCP} / a_g$ .

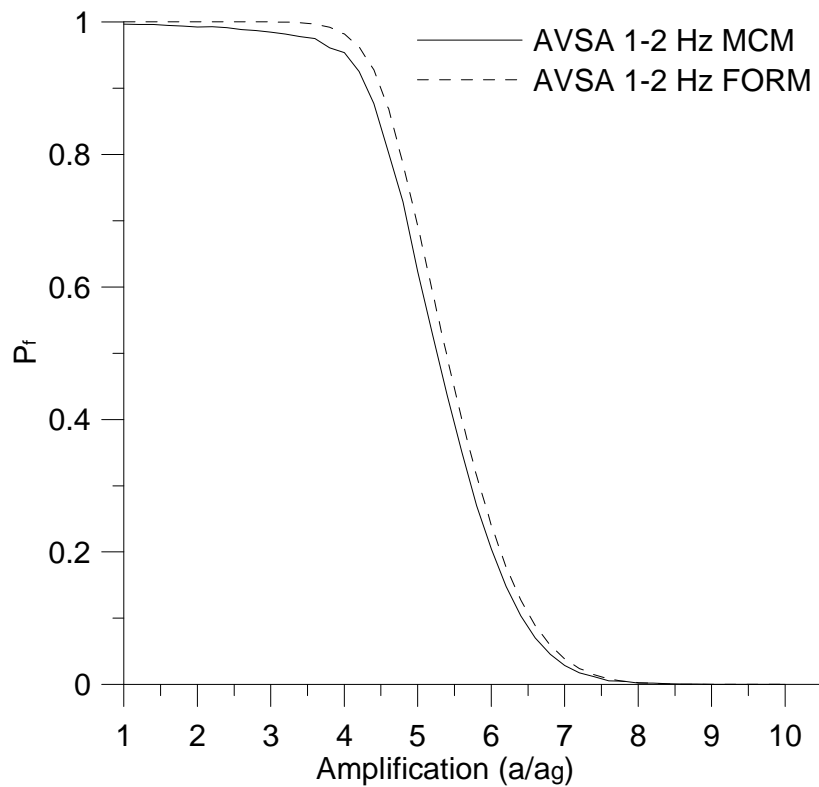
The AVSA functions emphasize the amplification of the response of a component; it shows how the probability of failure can be incremented when the peak acceleration of a component, averaged over a fixed range of natural frequencies, is considered. In the example here shown, the AVSA functions describe the fragility of a component located at RCP level when its main natural frequency is into the 1-2Hz or 2-5Hz frequency ranges.



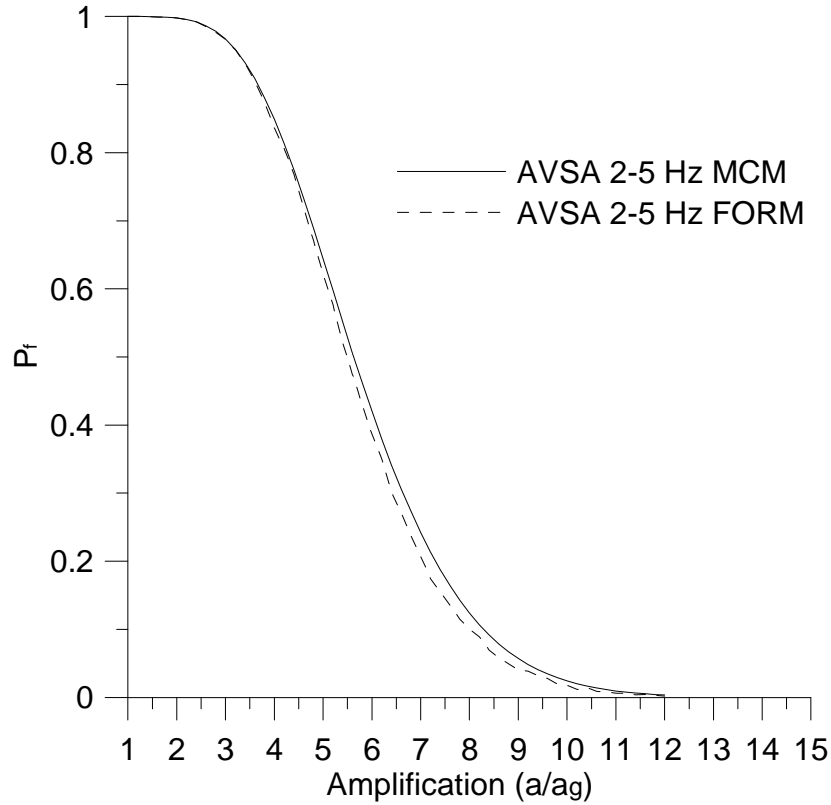
**Figure 22.** MCM fragility functions



**Figure 23.** RCP absolute acceleration. Fragility curves: MCM and FORM



**Figure 24.** AVSA 1-2 Hz. Fragility curves: MCM and FORM



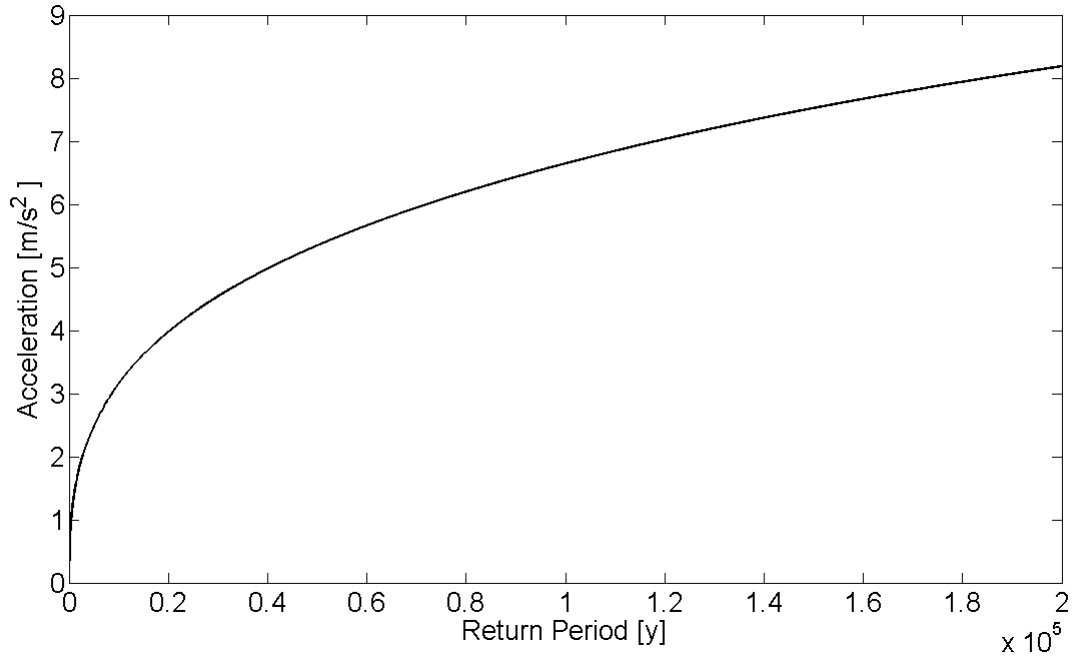
**Figure 25.** AVSA 2-5 Hz. Fragility curves: MCM and FORM

The application of FORM allows to compute the fragility functions in a alternative way. The probability of failure is computed, for each amplification, as the distance (from the origin) of the tangent plane to the limit state function at the design point.

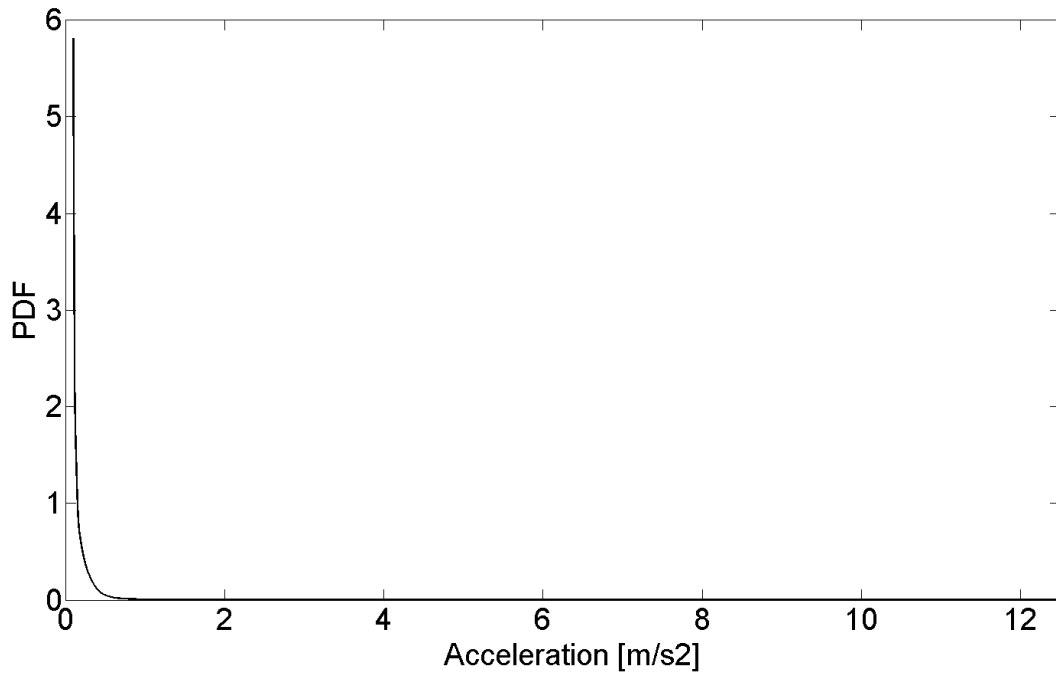
Once the design point is found, the evaluation of  $P_f$  is rapidly performed. The comparison between the three curves in Figure 22 is reported by Figures 23-25, respectively for the absolute acceleration, the AVSA 1-2Hz and 2-5Hz.

## 9. Application to the computation of seismic risk

The remaining of this report is devoted to the evaluation of the seismic risk by integrating the hazard and fragility evaluations. In particular it is considered the absolute acceleration fragility function as processed by FORM (Figure 23).



**Figure 26.** Seismic hazard

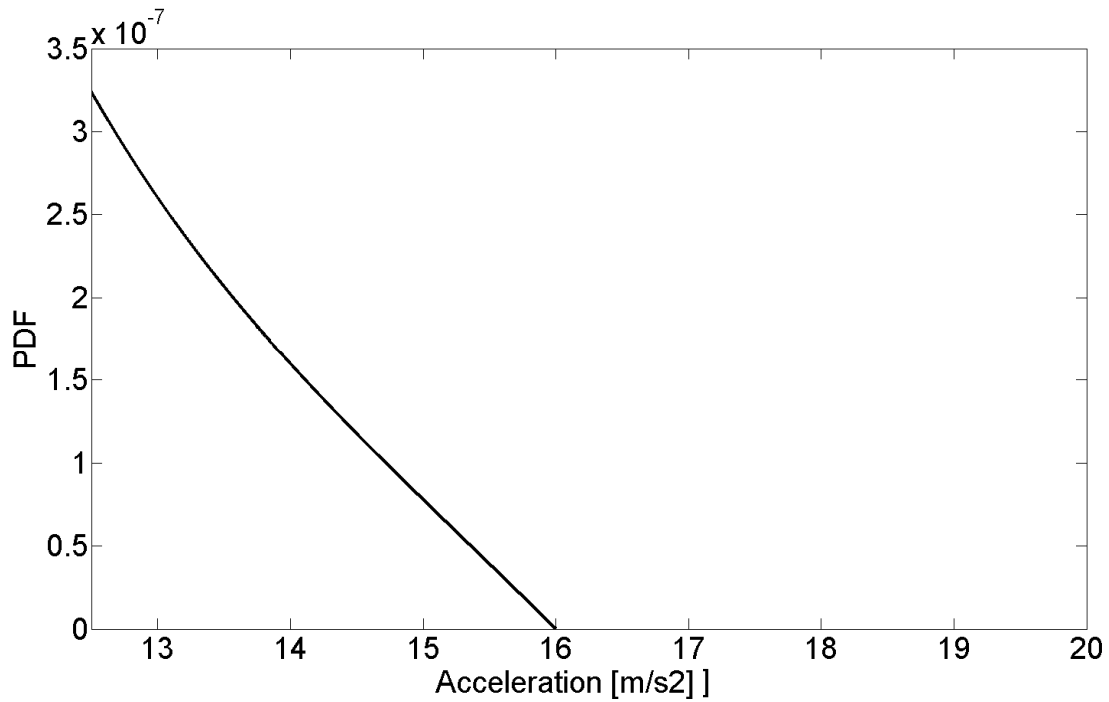


**Figure 27.** PDF

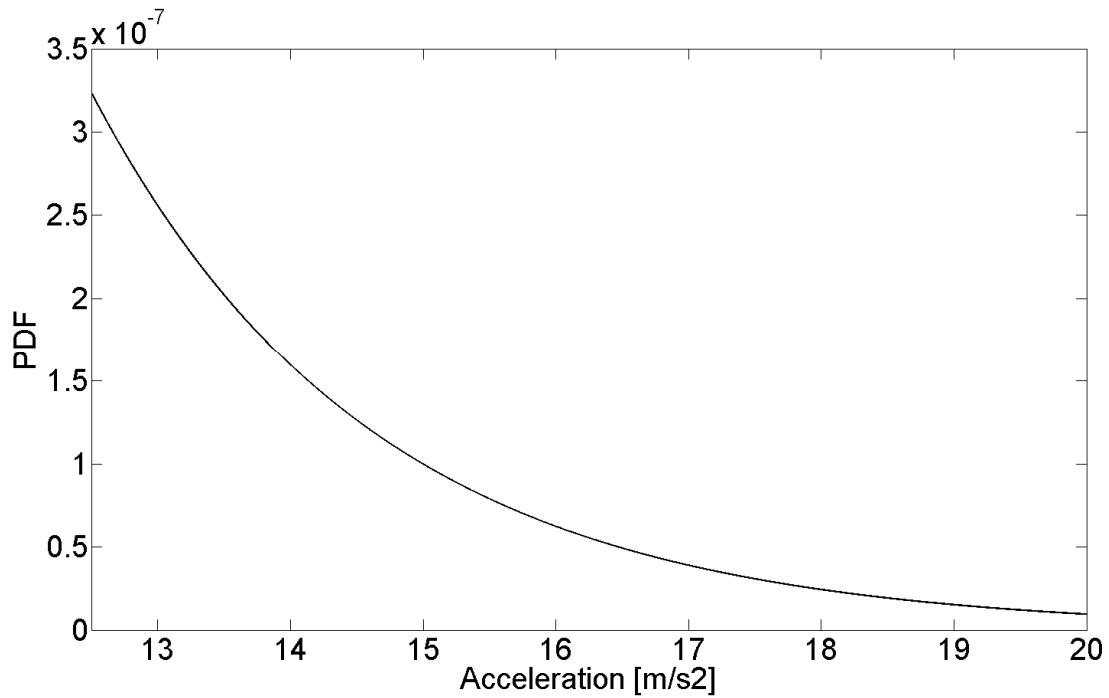
The problem of establishing the hazard curve is complex due to the fact the statistical parameters over a certain limit, in terms of return period, lacks of observable data. Therefore, some assumptions have been introduced. The hazard is related to a site described by return period vs ground acceleration in Figure 26.

In the estimation of the seismic risk two hypotheses has been introduced:

- 1) the PDF (probability density function, Figure 27) for the hazard is extended and truncated to  $16\text{m/s}^2$  (Figure 28);
- 2) the PDF is extended to  $20\text{m/s}^2$  and it is not truncated (Figure 29).



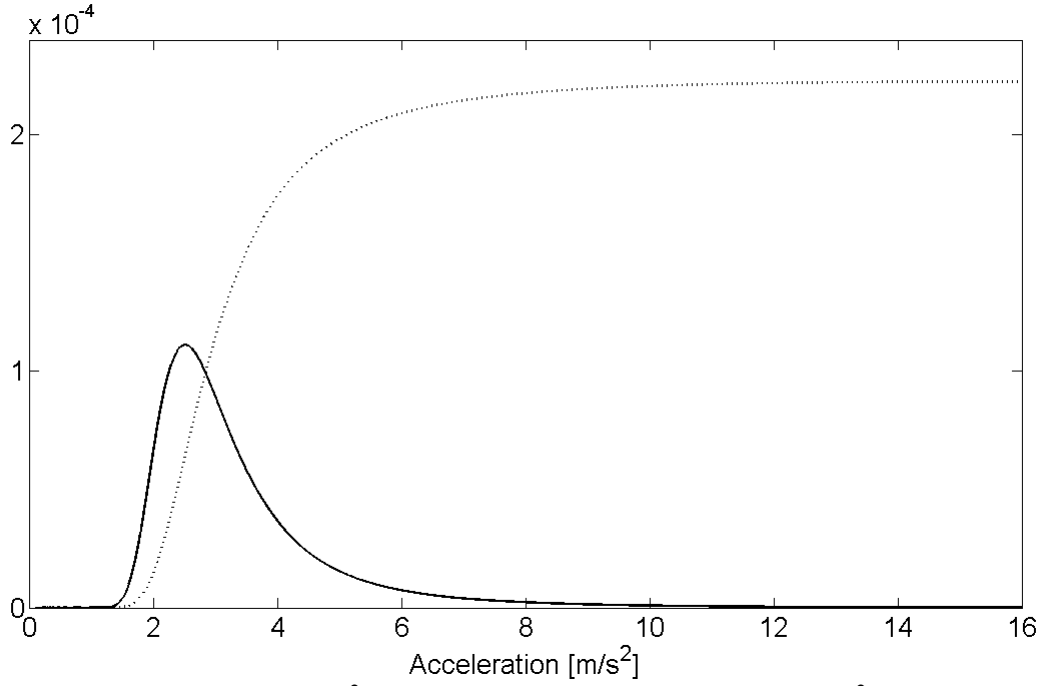
**Figure 28.** Detail: PDF extended and truncated to  $16\text{m/s}^2$



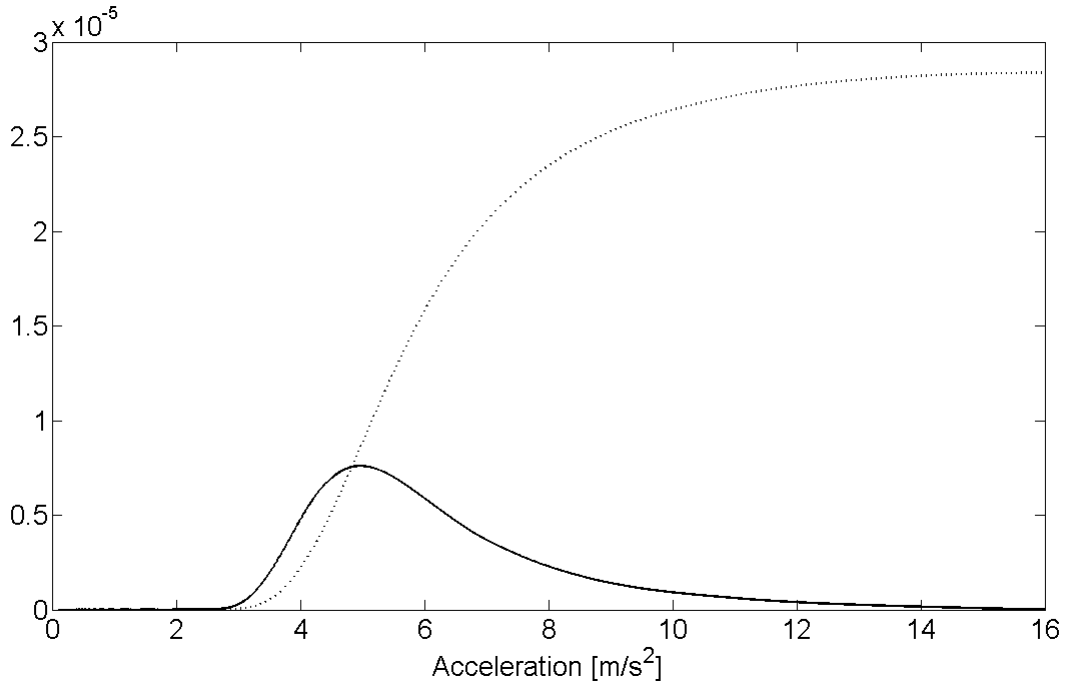
**Figure 29.** Detail: PDF extended to  $20\text{m/s}^2$

Following these two assumptions, the probability of failure has been computed for several failure accelerations ( $a_f$ ), related to a component at the RCP level. In particular  $a_f = 5, 10, 15, 20, 25, 30, 35, 40 \text{ m/s}^2$  have been considered. The results are reported for extended and truncated PDF in Figures 30-37; for extended PDF, with no truncation, in Figures 38-45. For the highest failure accelerations levels the failure probabilities obtained from the non-truncated PDF are only rough approximations, due to the fact the fragility times hazard function is non-zero in a wider acceleration domain.

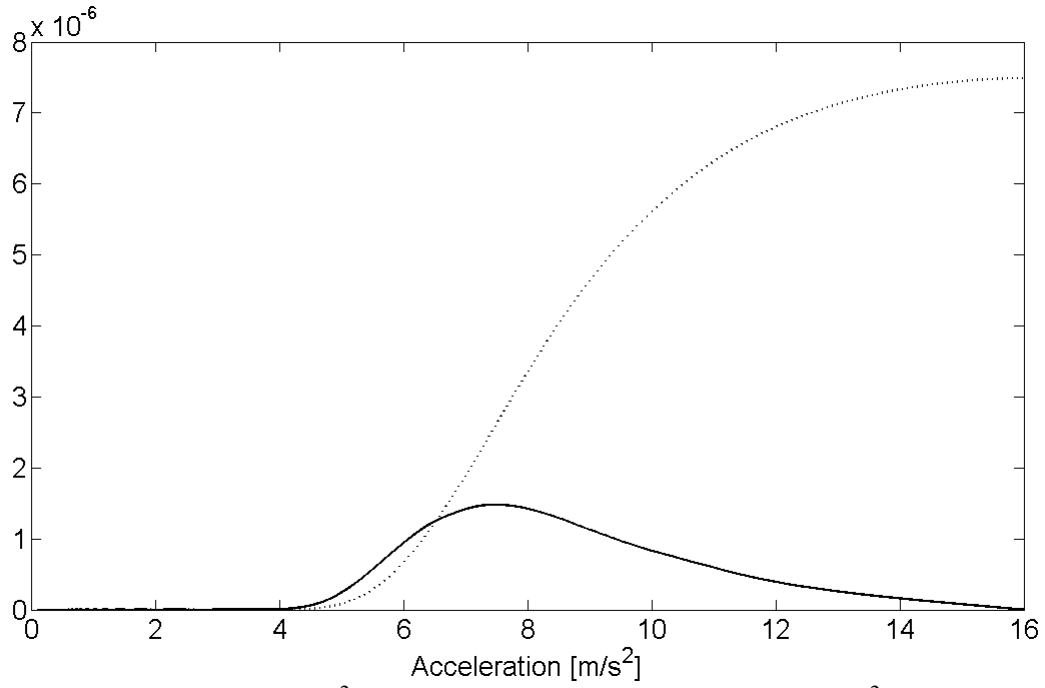
Table VII summarizes the probabilities of failure for the considered component acceleration thresholds.



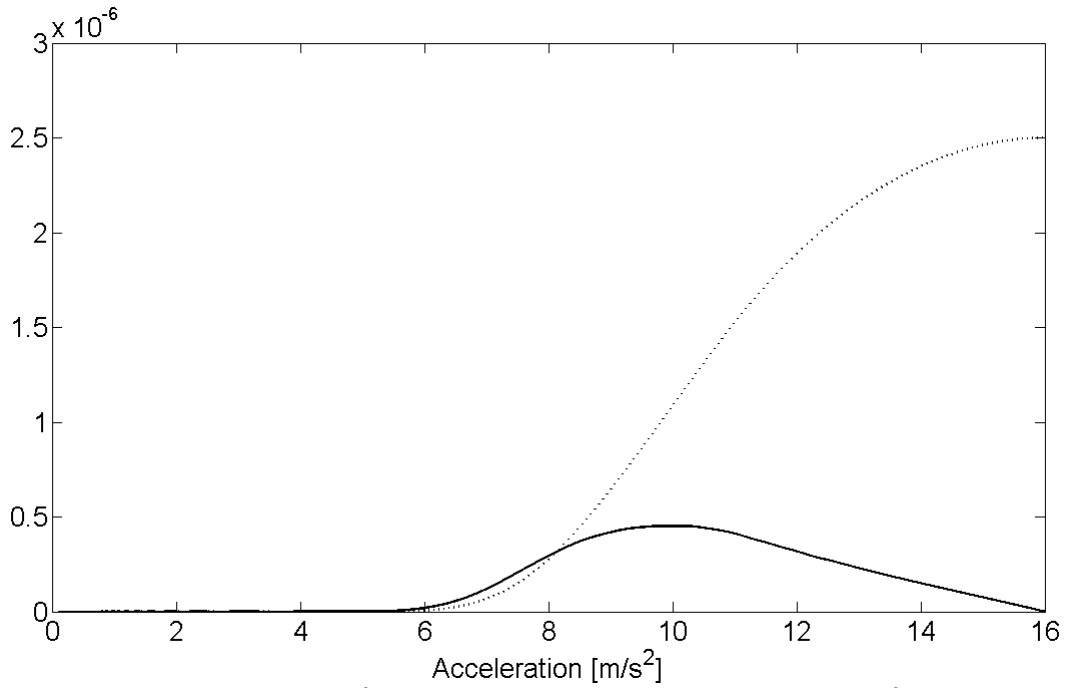
**Figure 30.**  $16\text{m/s}^2$  extended and truncated PDF  $a_f = 5\text{m/s}^2$ .  
Fragility times hazard vs  $pga$  and failure probability vs  $pga$  (dashed).



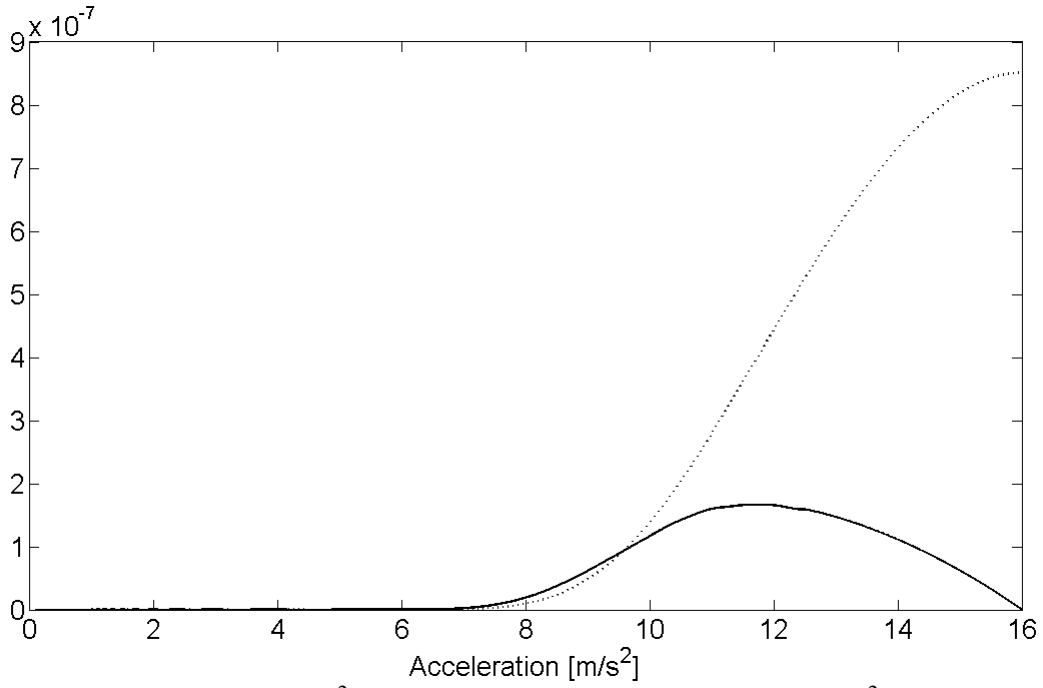
**Figure 31.**  $16\text{m/s}^2$  extended and truncated PDF,  $a_f = 10\text{m/s}^2$ .  
Fragility times hazard vs  $pga$  and failure probability vs  $pga$  (dashed).



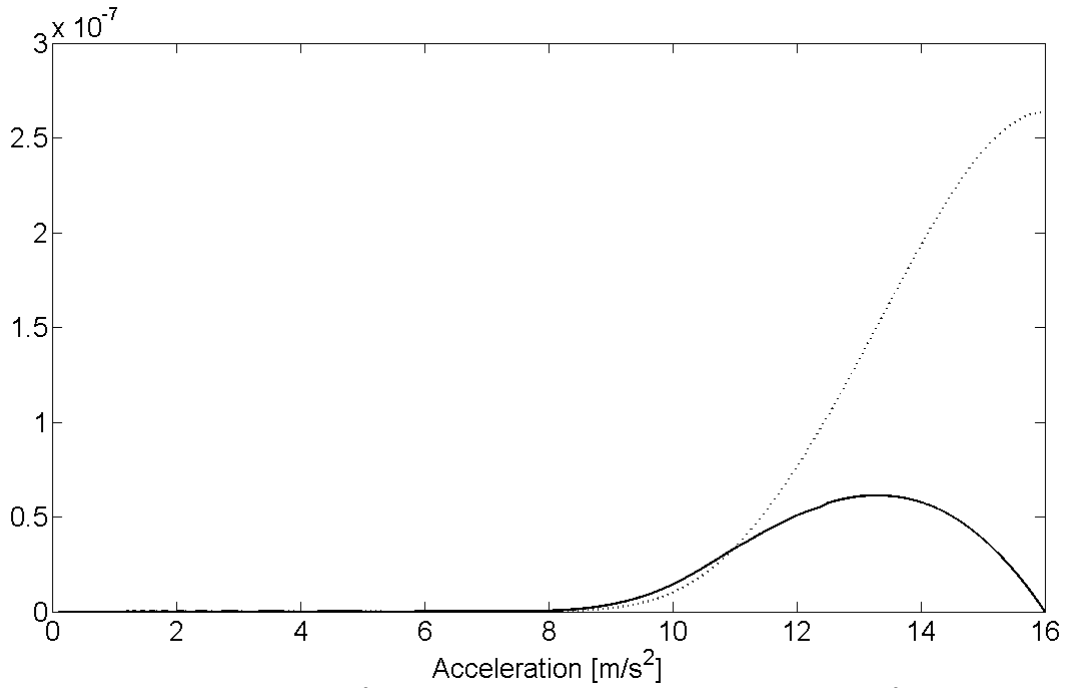
**Figure 32.**  $16\text{m/s}^2$  extended and truncated PDF,  $a_f=15\text{m/s}^2$ .  
Fragility times hazard vs  $pga$  and failure probability vs  $pga$  (dashed).



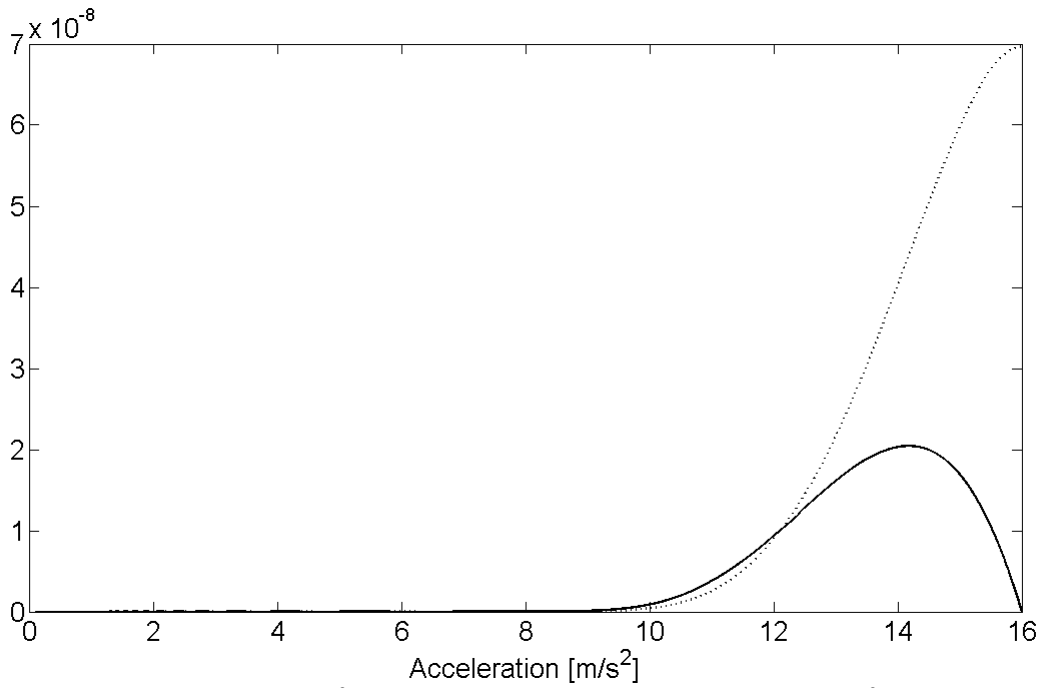
**Figure 33.**  $16\text{m/s}^2$  extended and truncated PDF,  $a_f=20\text{m/s}^2$ .  
Fragility times hazard vs  $pga$  and failure probability vs  $pga$  (dashed).



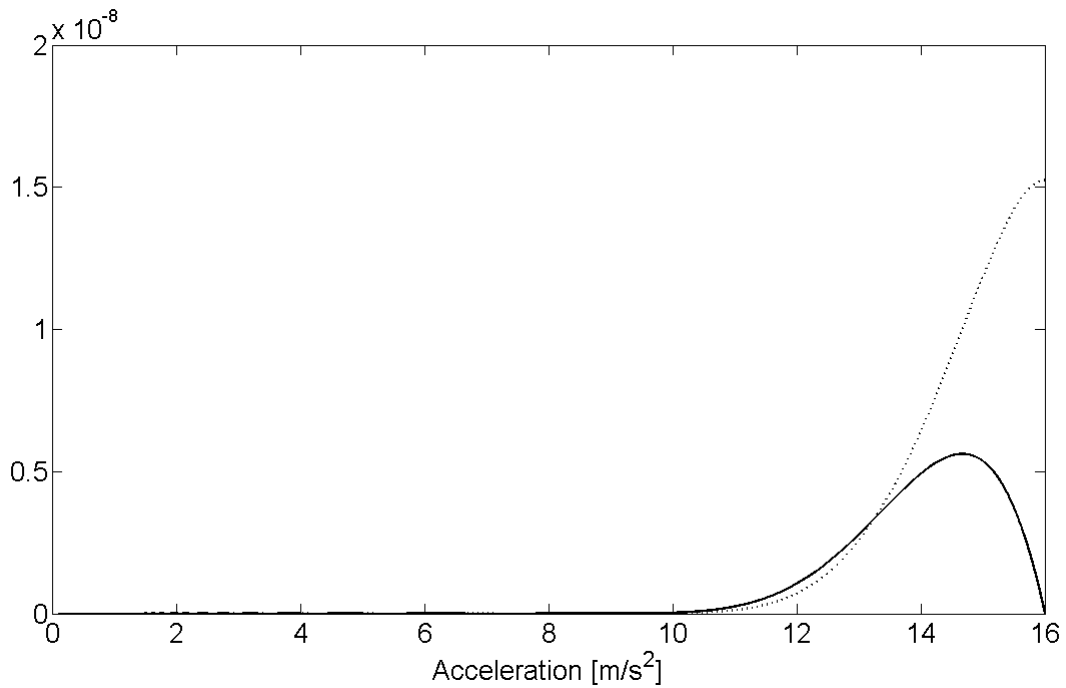
**Figure 34.**  $16\text{m/s}^2$  extended and truncated PDF,  $a_f = 25\text{m/s}^2$ .  
Fragility times hazard vs  $pga$  and failure probability vs  $pga$  (dashed).



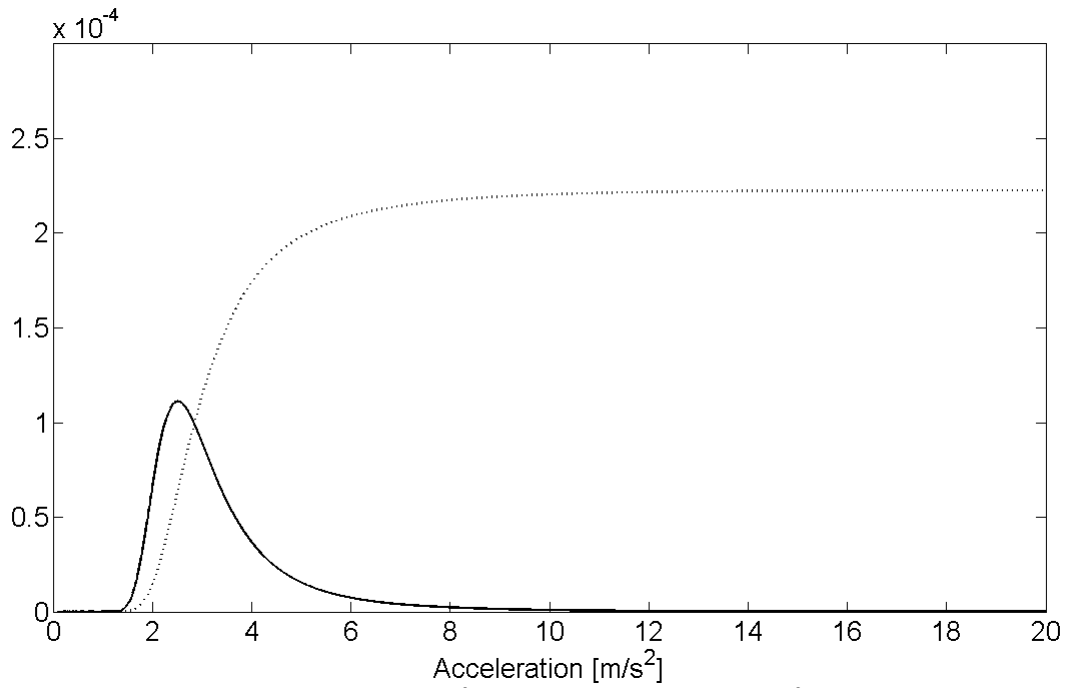
**Figure 35.**  $16\text{m/s}^2$  extended and truncated PDF,  $a_f = 30\text{m/s}^2$ .  
Fragility times hazard vs  $pga$  and failure probability vs  $pga$  (dashed).



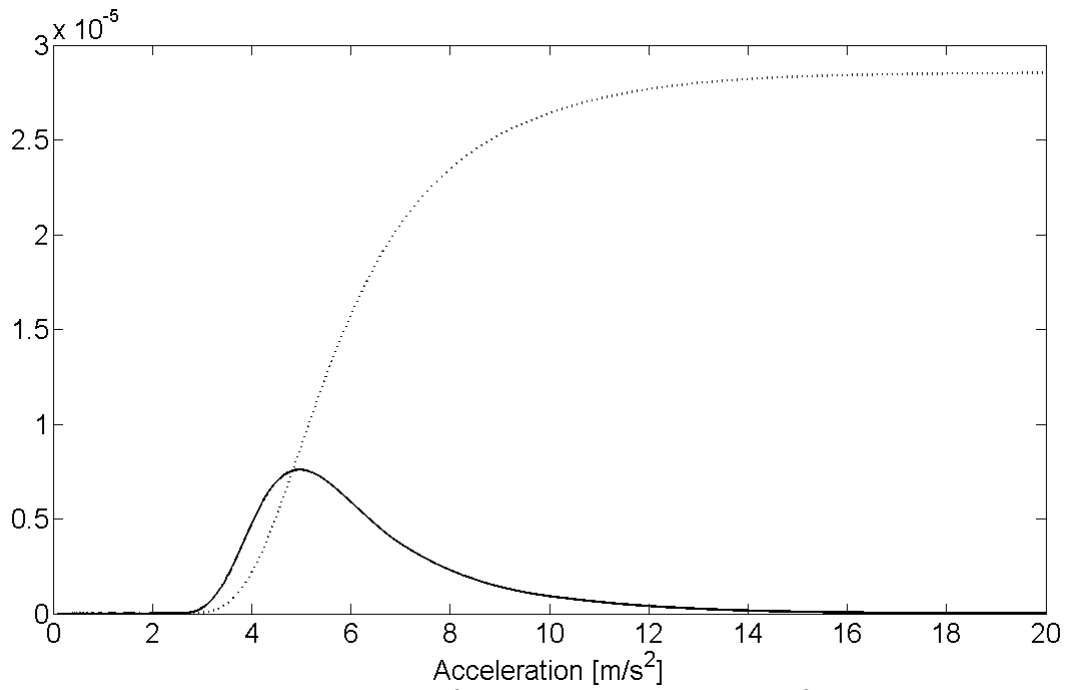
**Figure 36.**  $16\text{m/s}^2$  extended and truncated PDF,  $a_f=35\text{m/s}^2$ .  
Fragility times hazard vs  $pga$  and failure probability vs  $pga$  (dashed).



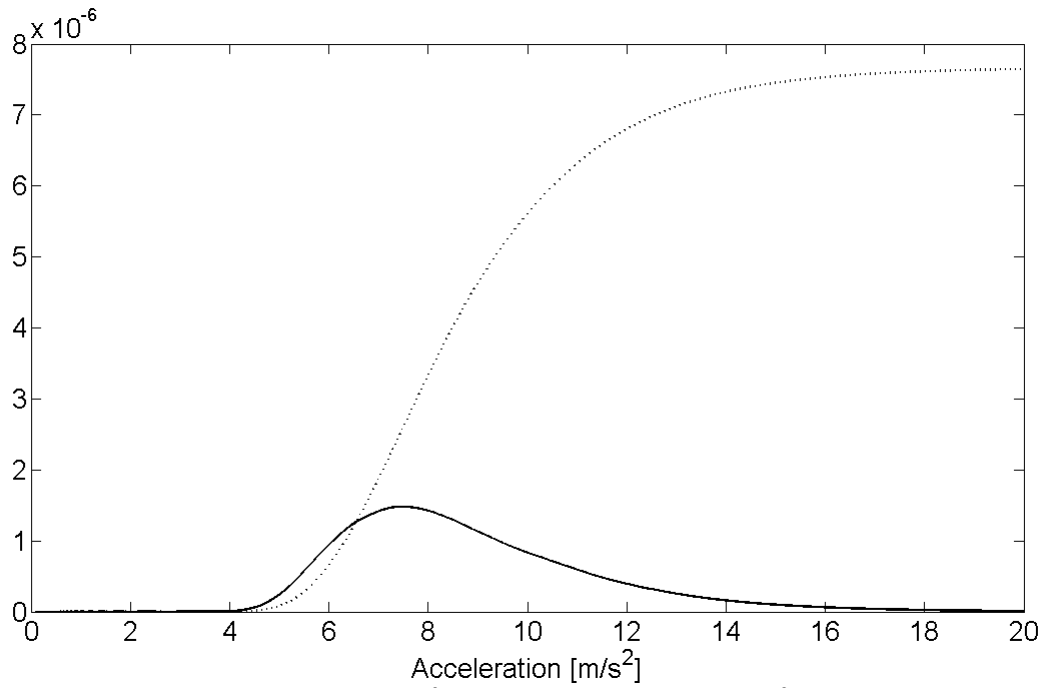
**Figure 37.**  $16\text{m/s}^2$  extended and truncated PDF,  $a_f=40\text{m/s}^2$ .  
Fragility times hazard vs  $pga$  and failure probability vs  $pga$  (dashed).



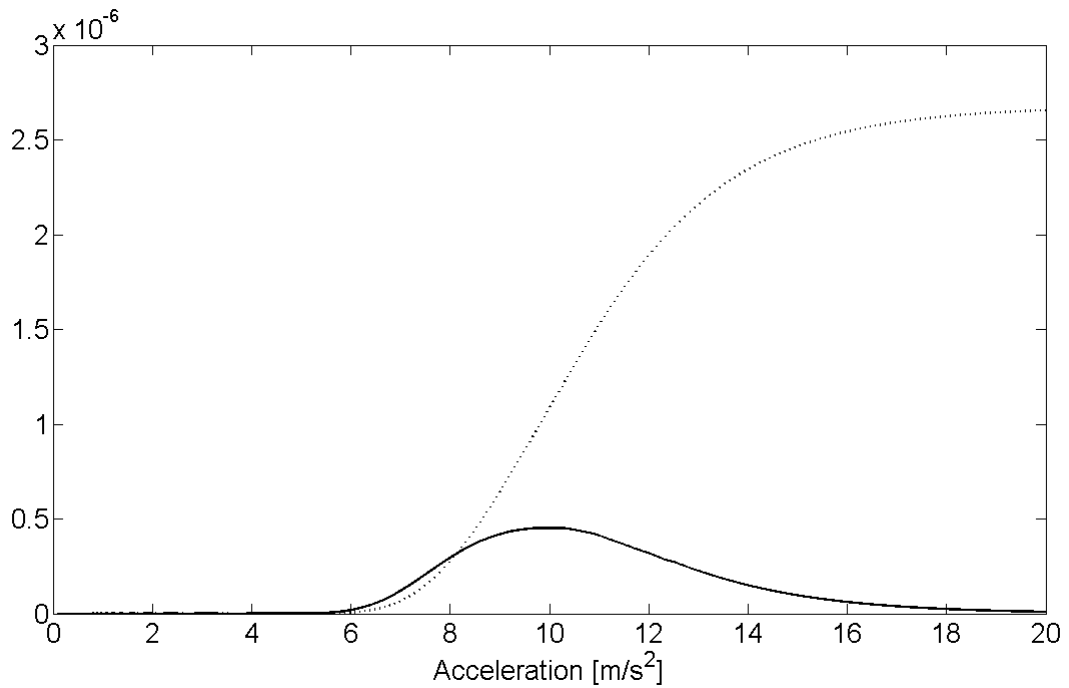
**Figure 38.**  $20\text{m/s}^2$  extended PDF,  $a_f = 5\text{m/s}^2$  .  
Fragility times hazard vs  $pga$  and failure probability vs  $pga$  (dashed).



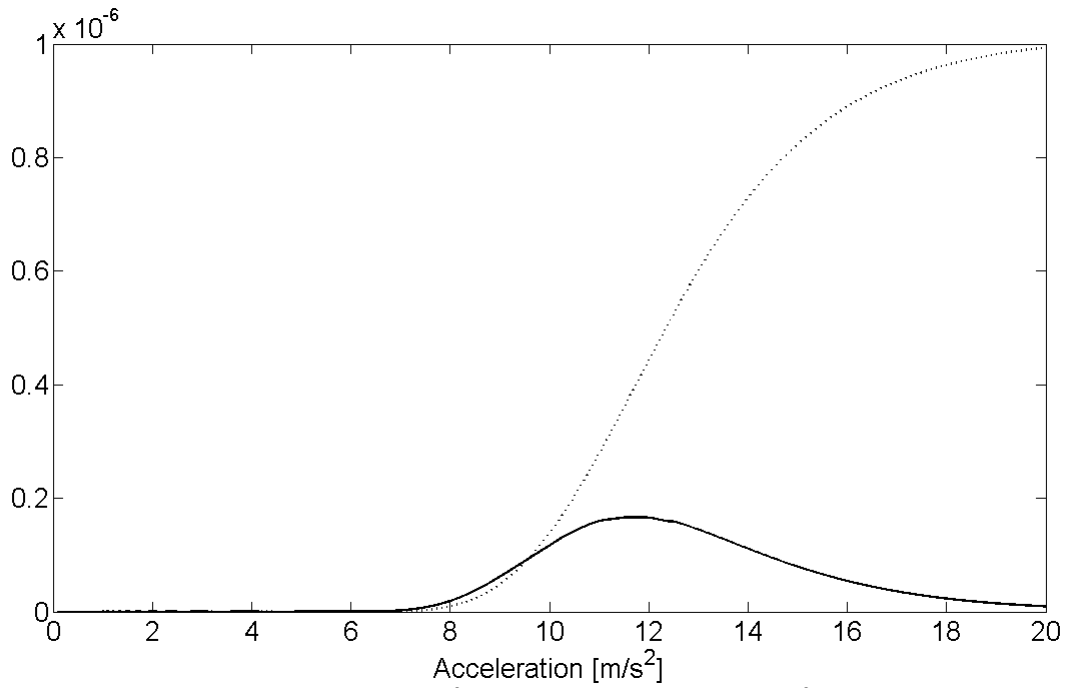
**Figure 39.**  $20\text{m/s}^2$  extended PDF,  $a_f = 10\text{m/s}^2$  .  
Fragility times hazard vs  $pga$  and failure probability vs  $pga$  (dashed).



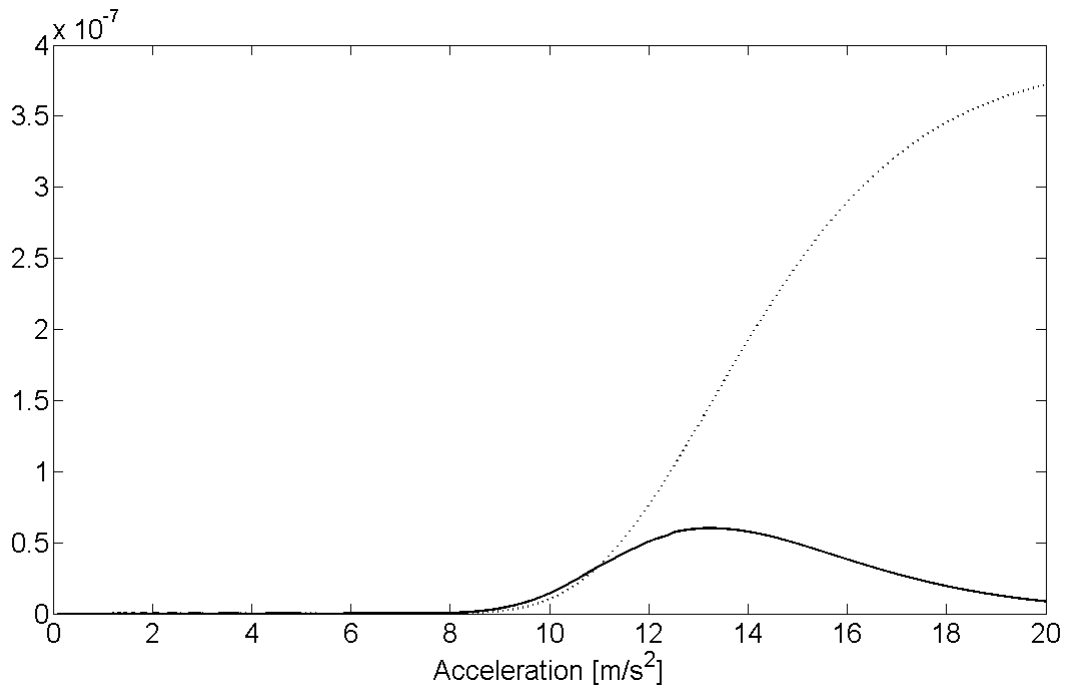
**Figure 40.** 20m/s<sup>2</sup> extended PDF,  $a_f = 15\text{m/s}^2$ .  
Fragility times hazard vs *pga* and Pf vs *pga* (dashed).



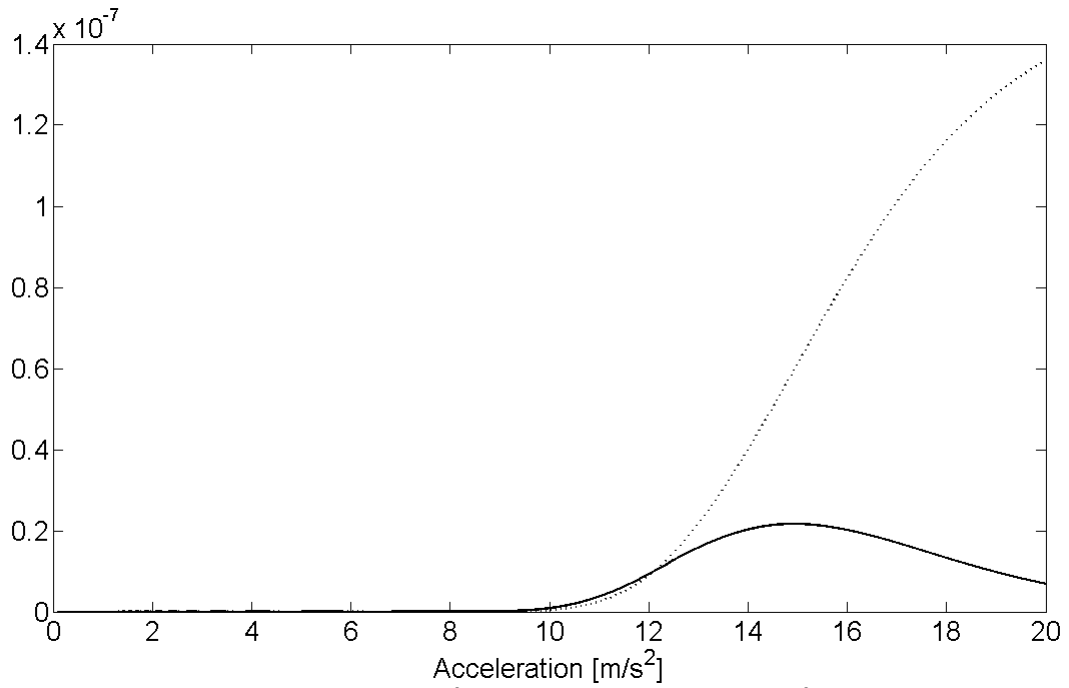
**Figure 41.** 20m/s<sup>2</sup> extended PDF,  $a_f = 20\text{m/s}^2$ .  
Fragility times hazard vs *pga* and failure probability vs *pga* (dashed).



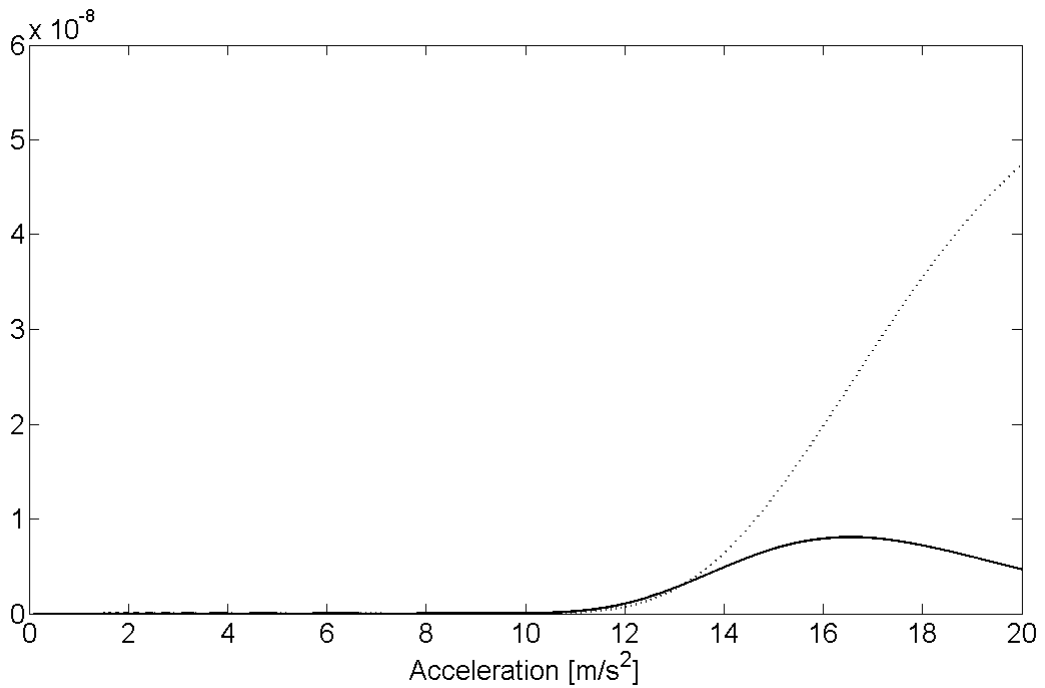
**Figure 42.** 20m/s<sup>2</sup> extended PDF,  $a_f = 25\text{m/s}^2$ .  
Fragility times hazard vs *pga* and failure probability vs *pga* (dashed).



**Figure 43.** 20m/s<sup>2</sup> extended PDF,  $a_f = 30\text{m/s}^2$ .  
Fragility times hazard vs *pga* and failure probability vs *pga* (dashed).



**Figure 44.**  $20\text{m/s}^2$  extended PDF,  $a_f = 35\text{m/s}^2$ .  
Fragility times hazard vs  $pga$  and failure probability vs  $pga$  (dashed).



**Figure 45.**  $20\text{m/s}^2$  extended PDF,  $a_f = 40\text{m/s}^2$ .  
Fragility times hazard vs  $pga$  and failure probability vs  $pga$  (dashed).

**Table VII.** Failure probabilities

$a_f$ [m/s <sup>2</sup> ]	$P_f$ (16m/s <sup>2</sup> extended and truncated PDF)	$P_f$ (20m/s <sup>2</sup> extended PDF)
5	2.22E-04	2.23E-04
10	2.84E-05	2.85E-05
15	7.49E-06	7.65E-06
20	2.50E-06	2.66E-06
25	8.51E-07	9.94E-07
30	2.64E-07	3.72E-07
35	6.97E-08	1.36E-07
40	1.52E-08	4.74E-08

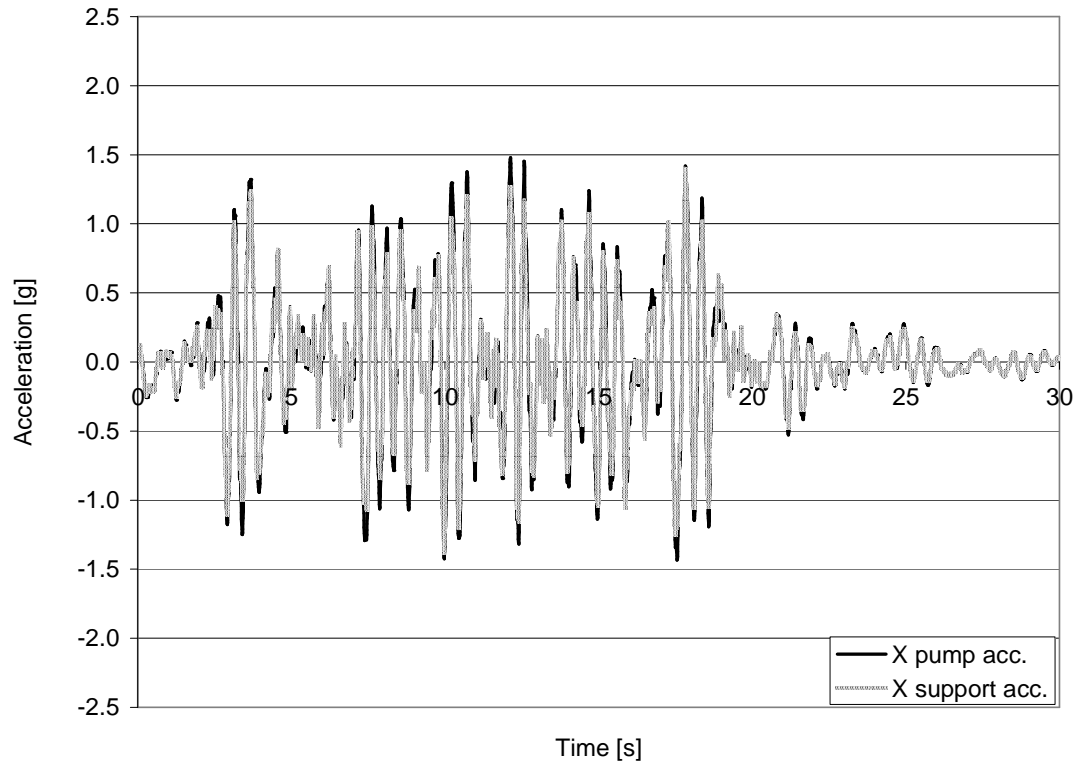
## 10. Conclusions

This study reports about the seismic risk computation of the not-isolated IRIS Reactor Building. A previously developed FE model of the Auxiliary Building is adopted and several random parameters are selected. The fragility analysis of the IRIS Reactor Building is then performed by consolidated analytical and numerical tools. The attention is focused at a point inside the vessel at the RCP level. The seismic risk is finally computed by considering an hazard curve related to a medium seismicity site with two different extended PDFs (truncated and not truncated). The resulting seismic risks, for both the hazard characteristics, points out that the new circular plant of the not-isolated IRIS has a lower seismic response than the previous version with rectangular plan (see also [1]); this is probably due to the large embedment, which has been explicitly modelled in the last version of the IRIS Reactor Building.

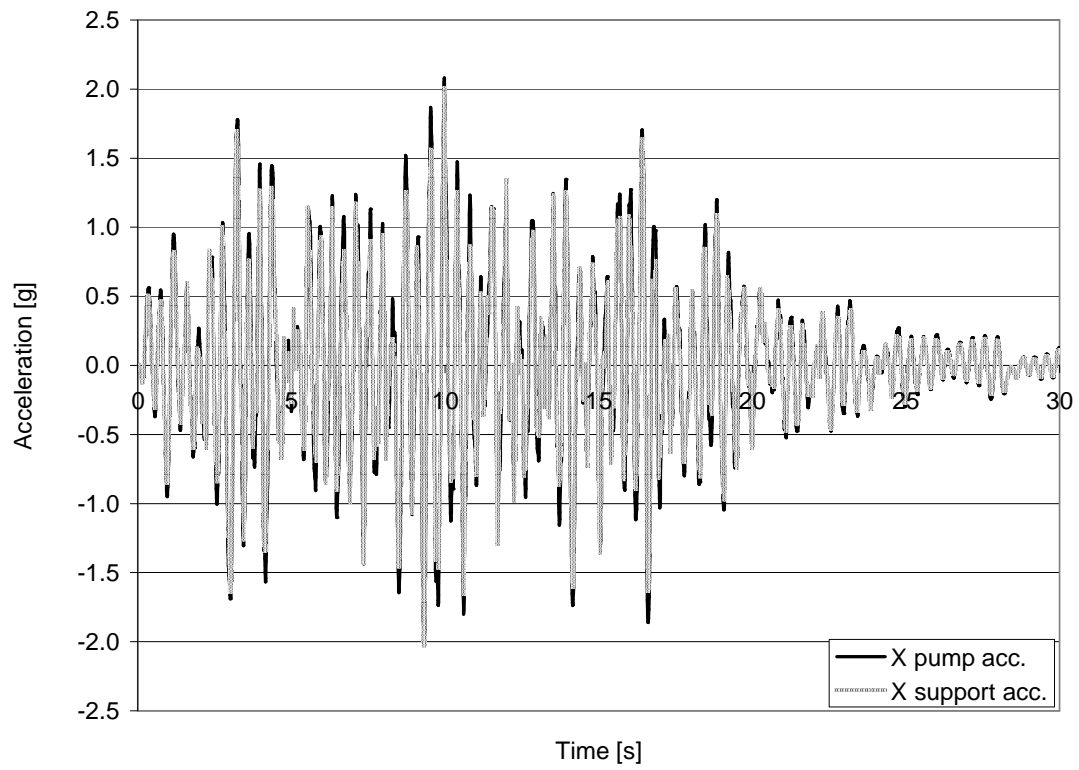
## References

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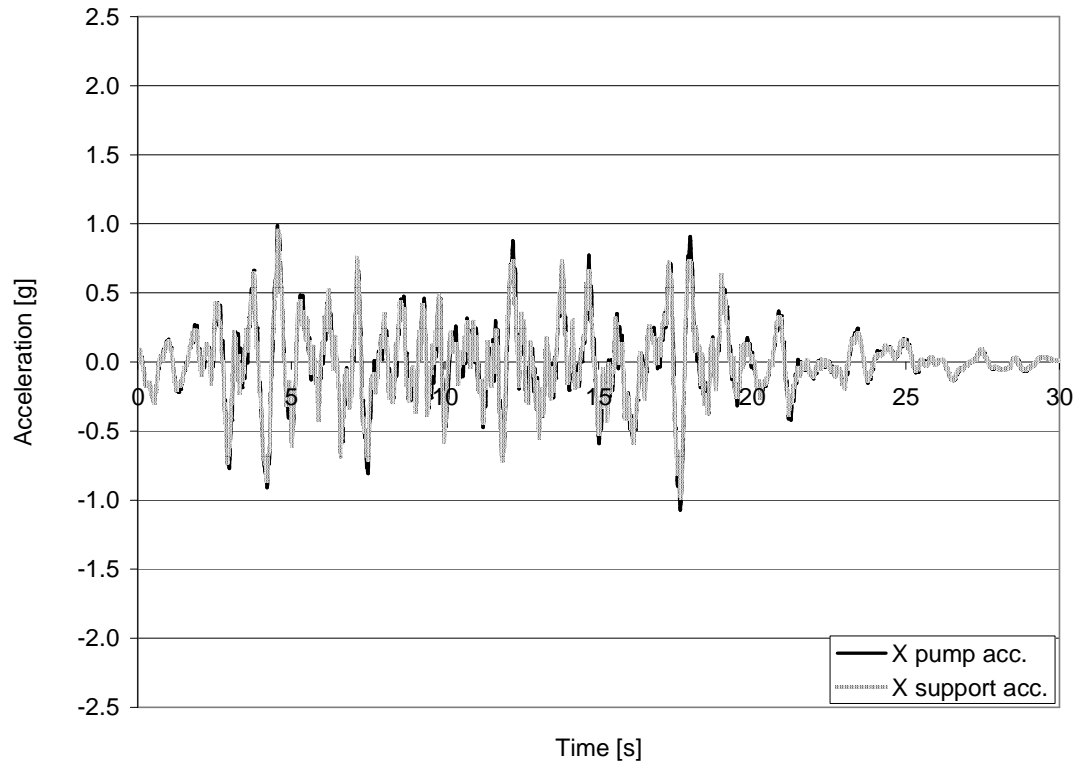
## APPENDIX A



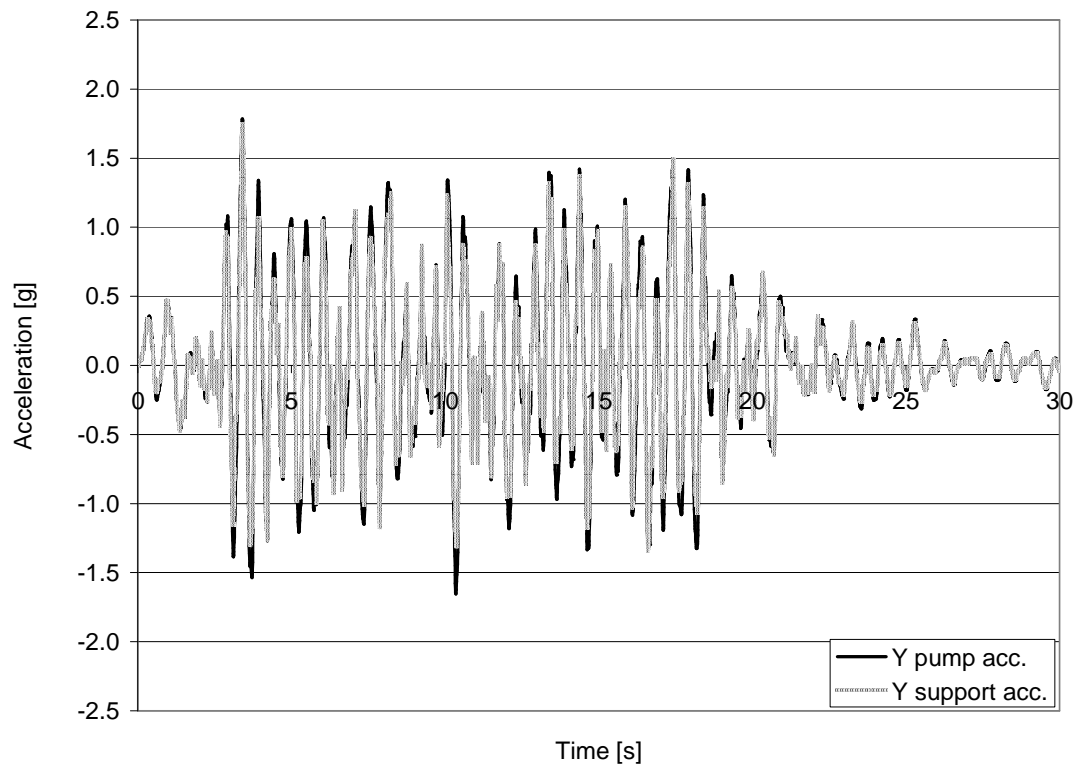
**Figure A1.** X direction absolute acceleration.  
Soil shear modulus  $G_s = 1$  ( $\nu_s = \nu_c = E_c = 1$ , Input Time History 1).



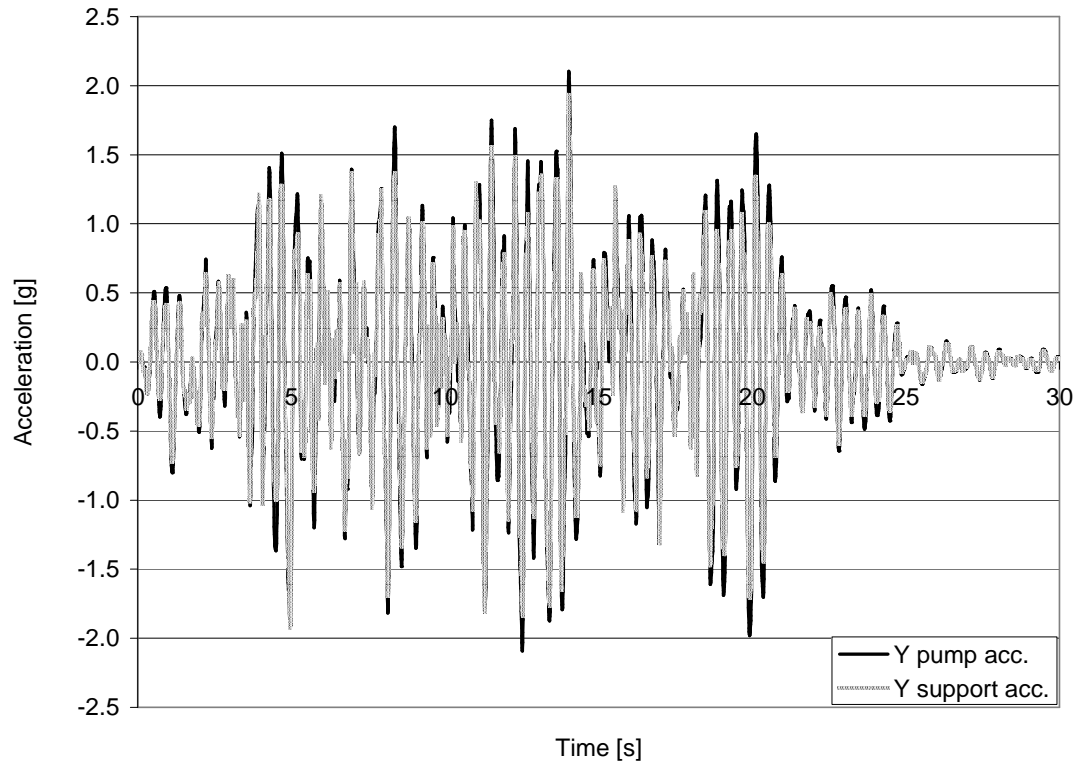
**Figure A2.** X direction absolute acceleration.  
Soil shear modulus  $G_s = 1.9$  ( $\nu_s = \nu_c = E_c = 1$ , Input Time History 1).



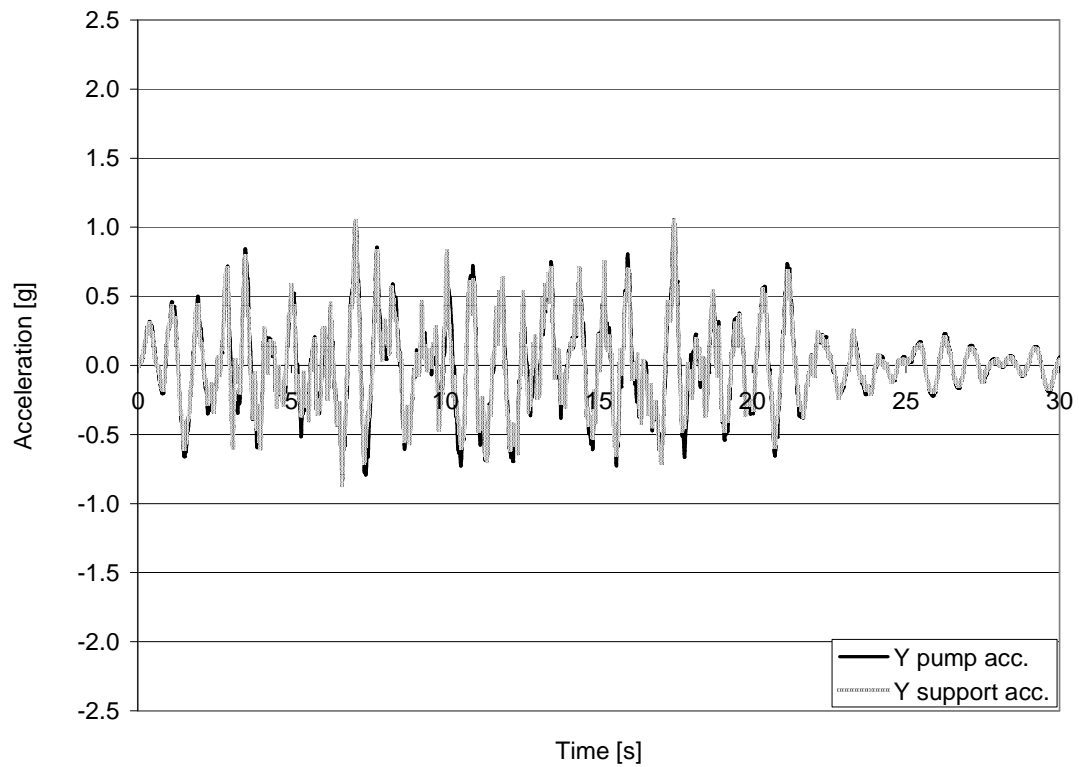
**Figure A3.** X direction absolute acceleration.  
Soil shear modulus  $G_s = 0.485$  ( $\nu_s = \nu_c = E_c = 1$ , Input Time History 1).



**Figure A4.** Y direction absolute acceleration.  
Soil shear modulus  $G_s = 1$  ( $\nu_s = \nu_c = E_c = 1$ , Input Time History 1).



**Figure A5.** Y direction absolute acceleration.  
Soil shear modulus  $G_s = 1.9$  ( $\nu_s = \nu_c = E_c = 1$ , Input Time History 1).



**Figure A6.** Y direction absolute acceleration.  
Soil shear modulus  $G_s = 0.485$  ( $\nu_s = \nu_c = E_c = 1$ , Input Time History 1).